

Scrapping, Renewable Technology Adoption, and Growth*

Bernardino Adao
Bank of Portugal

Borghan Narajabad
Federal Reserve Board

Ted Temzelides
Rice University

This Version: 8/5/2021

Abstract

We develop a dynamic general equilibrium integrated assessment model that incorporates scrapping costs due to new technology adoption in renewable energy, as well as externalities associated with carbon emissions and renewable technology spillovers. We use world-economy data to calibrate our model and investigate the effects of the scrapping channel on renewable energy adoption and on the optimal energy transition. Our calibrated model implies several interesting connections between scrapping costs, the two externalities, policy, and welfare. We investigate the relative effectiveness of two policy instruments; Pigouvian carbon taxes and policies that internalize spillover effects, in isolation as well as in tandem. Our findings suggest that scrapping costs are of quantitative importance for technology adoption and the energy transition. The two policy instruments are better thought of as complements rather than substitutes.

JEL Codes: H21, O14, O33, Q54, Q55

Keywords: Technology adoption, scrapping, energy transition, climate, dynamic taxation

*The opinions expressed in the paper do not necessarily reflect those of the Bank of Portugal or the Federal Reserve System. We are grateful to Antonia Diaz, participants at the Yale University Cowles Foundation Summer Conference on Macroeconomics and Climate Change, the Vienna Macro Conference, the CESifo conference on Energy and Climate Economics, the ASSA Meetings, and the SED Meetings for their comments on earlier versions of the paper.

1 Introduction

We investigate the optimal transition from a primarily fossil-fueled, to a renewable energy-fueled world economy. This transition depends on several components. First, fossil fuel sources constitute an exhaustible resource. A second consideration involves environmental factors. As fossil fuel use generates externalities through increasing the stock of greenhouse gas (GHG) emissions, the need for a clean substitute becomes increasingly apparent. In addition, technology spillovers imply the need to consider that investments in renewable technology create positive externalities. The main contribution of our paper lies in exploring the quantitative significance of an additional, not well-studied factor in the process of new renewable technology adoption. In the presence of rapid technological progress and large capital costs, new technology adoption often involves the scrapping of existing equipment. More precisely, when productivity is embedded in the capital stock, replacing existing capital in order to install more productive equipment implies certain additional costs.¹ The greater the speed of improvements, the higher the costs resulting from early adoption. Our modeling of this effect applies more generally, but we believe it is particularly relevant for energy investments, as they tend to be capital intensive and as renewable energy technologies are new and subject to relatively rapid technological progress as compared to fossil fuel. Our main contribution lies in exploring the quantitative significance of this channel in a dynamic general equilibrium integrated assessment model (IAM) that incorporates environmental and technological spillover externalities.

Although our aggregate modeling approach abstracts from individual sectors, the following example might be instructive of the kind of effect we have in mind. Consider the market for electric vehicles (EV). Batteries are a significant fraction of the cost (often close to 30-40%) of purchasing an EV. By any measure (including increased energy density, reduced cost, etc.) batteries have been steadily improving in recent years. Yet, in comparison, EV purchases have remained relatively flat over the same time horizon. It is important to note that for virtually all EV, the battery technology at the time of purchase is “embedded” in the vehicle. That is, it is difficult or impossible for it to be upgraded, unless the vehicle is scrapped and replaced with a new one. It is reasonable to expect that, concerned about characteristics such as overall range, some consumers might prefer to wait until sufficient progress justifies an EV purchase. This would be in line with our reasoning: there are costs associated with early adoption.²

¹These include costs associated with decommissioning, scrapping, or recycling old equipment, adjustment costs resulting from the switch, legal and transaction costs associated with financing, selling, purchasing, and installing new equipment, etc. Mauritzen (2012) discusses scrapping patterns for less productive wind turbines in Denmark. To our knowledge, our paper is the first to study the implications of these costs for optimal renewable energy investment in the context of a dynamic general equilibrium integrated assessment model.

²For more on EV see, for example, <https://www.eia.gov/todayinenergy/detail.php?id=36312#>, https://www.researchgate.net/figure/Evolution-of-battery-energy-density-and-cost-Global-EV-outlook-2016_fig3_309313559, and <https://www.statista.com/statistics/797638/battery->

A second focus of our study concerns the effectiveness of different environmental policy instruments. While Pigouvian taxes on carbon emissions have several theoretical advantages and are generally favored by economists, they have proved difficult to implement in practice. As a partial substitute, many advocate policies that directly promote market penetration by renewables. We investigate the degree of substitutability between carbon taxes and policies that internalize spillovers, thus, promoting renewable energy.

In our model, energy, capital, and labor are inputs in the production of final consumption goods. Energy can be produced from either fossil or renewable sources. Both require capital, which is also used in the production of the final good. At each point in time, productivity in the renewable energy production can increase as a result of adopting new capital. The actual improvement is subject to a spillover, as it depends on the aggregate investment in the renewable sector. We model the cost associated with scrapping and replacing existing equipment as a temporary adverse productivity shock to the production function of renewable energy firms. These costs are assumed to be proportional to the size of the capital replacement.

An important modeling choice concerns the degree of substitutability between different forms of energy. We will distinguish between substitutability in production versus in consumption of energy. We assume that, once produced, renewable and fossil fuel derived energy are perfect substitutes in the production of the final good. A high substitutability seems a reasonable benchmark when considering long-run effects, as we do in this paper. For example, substitutability is justified in the presence of energy storage.³ Importantly, fossil fuel and renewable forms of energy in our model are not perfect substitutes in terms of their required inputs, as they require different amounts of capital to produce. The evolving nature of renewable energy technologies will be a main focus, as we study properties of the optimal energy transition. While we do not consider technology advancements in fossil fuel in our benchmark case, We will investigate the robustness of our findings to introducing technological progress in the fossil fuel sector.

We employ an IAM to characterize the optimal transition to a renewable energy-fueled economy. The model is based on Golosov, Hassler, Krusell, and Tsyvinski (GHKT, 2014), who in turn build on Nordhaus's pioneering work in climate economics. We decentralize the optimum using a Pigouvian tax on GHG emissions together with a revenue neutral policy on renewable technology adoption and find that the efficient energy mix involves a gradual decline in the use of fossil fuel. We then calibrate the model using world economy data.

The extent to which the world economy will use its available fossil fuel reserves depends on the assumption about the total endowment of accessible hydrocarbons. For realistic parametrizations, the transition is made well before exhaustion of these resources. In the absence of a Pigouvian tax on carbon emis-

share-of-large-electric-vehicle-cost/. EV purchases are often subsidized, which we ignored for this discussion.

³While not widely available currently, there are strong indications that such storage technologies will enter commercialization in the next decade or so.

sions, policies that incentivize penetration by renewables through internalizing spillovers may provide relatively small benefits, and can even be detrimental to short run growth. In addition, we find that the decrease in global temperatures with respect to the status quo is negligible under this policy. In contrast, global temperatures decrease by about 10 percent if the optimal Pigouvian tax is in place. Similarly, the reduction in consumption of fossil fuel resulting from internalizing technology spillovers is significantly larger if the optimal Pigouvian tax is also in place. While the gains from internalizing the spillovers alone are small, comparing the status quo to the scenario where both policies are implemented results in a consumption-equivalent welfare gain of 1.431 percent. We conclude that when it comes to social welfare, carbon taxes and policies that promote renewable energy by eliminating spillover externalities are best thought of as *complements* rather than substitutes.

While theoretically desirable, Pigouvian taxes have generally proved difficult to implement in practice. For example, a short-lived government might choose a lower or no Pigouvian tax, as it is effectively more impatient than the representative agent. In the Appendix, we briefly discuss how the theoretical model can be extended to account for such considerations. The urgency of climate change has led to calls for action by several international organizations and governments around the globe. As a variety of mitigation measures are currently under consideration, our findings suggest that, in the presence of rapid technological progress and scrapping costs, some caution might be warranted before we conclude that direct subsidies are always a suitable substitute in the absence of a carbon tax.

1.1 Quantitative Modeling

Four parameters will be important for our calibration strategy: (1) the level of the spillover externality in renewable energy production, (2) the current “Pigouvian tax rate” (the ratio of the actual carbon tax relative to its optimal value), (3) the initial resources of fossil fuel, and (4) the productivity in the renewable energy technology. To calibrate these parameters, we will use observations from the world economy, together with theoretical relationships derived in the context of our model. For example, we will employ the fact that the change in the renewable energy share of the energy output decreases in the level of the spillover externality. Similarly, to get a handle on the current Pigouvian tax rate, we use the current level of fossil fuel consumption and the implication that an increase in the Pigouvian rate would result in a decrease in fossil fuel use. Importantly, the magnitude of the Pigouvian tax in our calibration should be interpreted as reflecting the difference between the opportunity cost of the average fossil fuel producer (which is rather low) and the average price paid by consumers of fossil fuel. Last, to calibrate the productivity in the renewable energy sector, we will use the current share of renewables together with the fact that their productivity is increasing in their share.

Our calibrated model allows us to derive several interesting connections between scrapping costs, the two externalities, Pigouvian taxation, growth, and

welfare. We investigate the quantitative importance and potential complementarity between the two policy instruments, by studying their effects in isolation and in tandem. Our findings suggest that scrapping costs are of quantitative importance when it comes to new technology adoption along the energy transition. We find that when spillover externalities are internalized, renewable firms take on capital at a smaller scale, as they need to scrap more of their capital in order to adopt newer technologies faster. This is due to the crucial assumption that the cost of technology adoption is proportional to the firm’s capital stock. Our results also point to complementarities between carbon taxes and internalizing spillovers, with sizable welfare gains only in the case when both policies are present.

As a robustness check, we calibrate the model taking into account technological developments in the fossil fuel sector. The calibrated magnitude of the Pigouvian tax remains virtually unchanged, but the value of the spillover externality is greater than in the benchmark case. We find that incorporating fossil fuel growth results in a faster transition to a fully renewable economy in the status quo case, and a lesser welfare gain from switching to the optimal technology adoption (since the calibrated value is already closer to the optimal level). Importantly, the main mechanisms governing the interactions between Pigouvian taxation and renewable technology adoption, which are the focus of our paper, remain intact when technological progress in fossil fuel is incorporated.

1.2 Related Literature

Our paper contributes to the growing literature that uses IAM to study energy transitions, innovation, and growth. In the economic growth literature, Parente (1994) studied a model in which firms choose to adopt new technologies as they gain specific expertise through learning-by-doing. He identified conditions under which equilibria exhibit constant per capita output growth. As in most of the literature on innovation and growth, Parente abstracted from issues related to climate and energy, which are the focus of our study. Atkeson and Burstein (2015) study the impact of policy-induced changes in innovative investment and the implications for medium-and long-run innovation and growth. They too abstract from climate and energy considerations.

Nordhaus (1994) pioneered the study of climate factors in dynamic economic modeling. Traditionally, most economic analysis of energy and environmental issues focuses on computable general equilibrium models which often abstract from endogenous technological progress.⁴ Acemoglu et al (2012) study a growth model that takes into consideration the environmental effects from operating “dirty” technologies. They consider policies that tax innovation and production in the dirty sectors. They find that subsidizing research in the “clean” sectors can speed up environmentally friendly innovation without the corresponding slowdown in economic growth. Consequently, optimal behavior in their model implies an immediate increase in clean energy R&D, followed by a complete

⁴See, for example, Nordhaus and Boyer (2000) and references therein.

switch toward the exclusive use of clean inputs in production. We view our paper as complementary to theirs. We do not model directed technical change and we instead introduce the scrapping-cost channel associated with new capital adoption. While we think that their main recommendations are likely to remain valid in the presence of scrapping, our quantitative findings suggest that the optimal rates of new technology adoption might be affected if we take such costs into account.

As mentioned earlier, our analysis builds on GHKT (2014). They develop a tractable dynamic general equilibrium model that incorporates the feedback between energy use and the resulting climate consequences. They derive a formula and numerical values for the optimal tax on carbon emissions. They, however, abstract from the costs associated with endogenous technological progress. We will employ several elements from their work in what follows, including the tractable modeling of the environmental externality. Van der Ploeg and Rezai (2016) extended the model in GHKT in several ways. They allow for general fossil fuel extraction costs, a negative impact of climate change on growth, mean reversion in climate damages, labor-augmenting and green technology progress, and a direct effect of the emissions stock on welfare. They discuss the social optimum, as well as the optimal carbon tax and renewable energy subsidies.⁵

Acemoglu, Akcigit, Hanley, and Kerr (2016) use the structure in GHKT to study questions related to the transition to clean technologies. They employ a “ladder” model to study technological progress in both the clean and the dirty sectors, and they estimate their model using R&D and patent data. They assume that increased representation of fossil fuel encourages further use, and that fossil fuel use stops after 200 years. They conclude that both Pigouvian taxation and renewable energy subsidies are needed in order to make the (optimal) transition sooner rather than later. The reason is that subsidies encourage technological progress without overtaxing short-run future output.

Fried (2018) develops a dynamic general equilibrium model to investigate the effect of carbon taxes in inducing innovation in green technologies. The carbon tax is chosen exogenously to match a 30 percent reduction in emissions in 20 years. The model introduces endogenous innovation in both dirty and green energy production, as well as in the non-energy sectors and assumes positive spillovers between clean and dirty energy technologies. As a result, the paper finds that abstracting from endogenous innovation results in overestimating the size of the carbon tax needed to attain the given reduction in emissions. More recently, Hassler et al (2020) introduce a multi-region general-equilibrium integrated assessment model. Their focus is on sub-optimal climate policies that may vary across regions. They consider the uncertainty associated with evalu-

⁵Other related papers include Stokey (1998), who considers growth under environmental constraints, Goulder and Schneider (1999), who study endogenous innovations in abatement technologies, Van der Zwaan et al, (2002), who investigate the impact of environmental policies in a model with learning-by-doing, and Popp (2004), who considers innovation in the energy sector and the costs of environmental regulation. See also Hartley et al (2016), who study technological progress and the optimal energy transition, and Van der Ploeg and Withagen (2011), who points to the possibility of a green paradox in this context.

ating the cost from climate change and find that the costs of underestimating climate change are an order of magnitude larger than the costs of overestimating it. Thus, when various energy sources are sufficiently substitutable, ambitious climate policies can be thought of as effective insurance against adverse climate shocks. Their analysis shows that the economic costs of achieving climate goals increase substantially when some regions do not participate in mitigation. Finally, they find that when it comes to climate goals, green energy subsidies are a poor substitute for a Pigouvian tax on fossil fuel, particularly on coal. Their model does not explicitly study endogenous technical change.

Gowrisankaran and Rysman (2012) explore a similar argument to ours in a different context. They study optimal decisions by consumers choosing the timing of purchase among an expanding set of available camcorders. As prices, quality, and variety improve over time, waiting is valuable in their model. In addition, while consumers usually hold only one camcorder at a time, they may substitute a new camcorder by scrapping an old one. They argue that initial market share for digital camcorders was not higher because forward-looking consumers were rationally expecting that cheaper and better players would appear in the future. A related effect is explored in Manuelli and Seshadri (2014). Their focus is in technology diffusion of tractors in American agriculture during the first part of the 20th century. They argue that part of the reason for the slow rate of adoption was that tractor quality kept improving over that period. As a result, farmers chose to postpone their purchase, rather than investing in a tractor that would soon become obsolete. The main contribution of our paper is to explore this channel in the context of renewable energy technology adoption.

The paper proceeds as follows. Section 2 introduces the model. Sections 3 and 4 discuss efficiency, equilibrium, and optimal policy. Section 5 outlines our calibration strategy. Section 6 presents our main quantitative findings, including those from an extension of the base model that accounts for productivity improvements in the fossil fuel sector. A brief conclusion follows. The Appendix contains technical material and some extensions.

2 The Base Model

We build an IAM that incorporates a version of the neoclassical growth model, together with energy, technology, and climate factors. Time is discrete and the horizon is infinite, $t = 0, 1, \dots$. There is a single consumption good per period, and all markets are competitive. The economy is populated by a representative infinite-lived household which discounts the future at rate $\beta \in (0, 1)$ and values period- t consumption, c_t , through a utility function $u(c_t)$. We assume that u is smooth, strictly increasing, strictly concave, and that the usual Inada conditions hold. The labor endowment is normalized to 1, and labor is supplied inelastically. There are three different types of firms, all owned by the household: the final-good firm, and two types of intermediate-good firms that produce energy from fossil fuel and from renewable sources, respectively. In each period, the household chooses how much capital, k_t , to rent at rate r_t and receives profits

resulting from the firms' activities. All capital depreciates at rate $\delta \in (0, 1)$.

The representative final-good-producing firm produces output, y_t , using capital, k_t^c , labor, l_t , and energy, e_t . Production can be affected by environmental quality, indexed by Γ_t , which reflects the total stock of greenhouse gases (GHG) in the atmosphere. Ignoring environmental damages, the final-good production function is given by

$$y_t \leq F(k_t^c, l_t, e_t, \Gamma_t). \quad (1)$$

We assume that environmental quality, Γ_t , affects output through a damage function $D_t(\Gamma_t)$, and that damages are multiplicative. Thus, the final good production function becomes

$$F(k_t^c, l_t, e_t, \Gamma_t) = (1 - D_t(\Gamma_t))\tilde{F}(k_t^c, l_t, e_t), \quad (2)$$

where $1 - D_t(\Gamma_t) = \exp[-\pi_t(\Gamma_t - \bar{\Gamma})]$. Here, $\bar{\Gamma}$ represents the pre-industrial GHG concentration in the atmosphere, and π_t is a variable that parametrizes the effect of higher GHG concentrations on damages. The function D captures the mapping from the stock of GHG, Γ_t , to economic damages measured as a percentage of output. We assume that $\tilde{F}(k_t^c, l_t, e_t)$ has a Cobb-Douglas form:

$$\tilde{F}(k_t^c, l_t, e_t) = \tilde{A}_t(k_t^c)^{\theta_k}(l_t)^{\theta_l}(e_t)^{1-\theta}, \quad (3)$$

where \tilde{A} is a productivity parameter, while θ , θ_k , $\theta_l \in (0, 1)$, and $\theta_k + \theta_l = \theta$. Thus, the final good production function can be rewritten as

$$y_t \leq A_t(k_t^c)^{\theta_k}(l_t)^{\theta_l}(e_t)^{1-\theta}, \quad (4)$$

where $A_t \equiv (1 - D_t(\Gamma_t))\tilde{A}_t$. The level of GHG evolves according to

$$\Gamma_t - \bar{\Gamma} = \sum_{n=0}^{t-T} (1 - d_n)f_{t-n}, \quad t \geq T, \quad (5)$$

where $d_n \in [0, 1]$, and f_{t-n} indicates the anthropogenic GHG emissions in period $t - n$. The variable $1 - d_n$ represents the amount of carbon that remains in the atmosphere n periods into the future and T defines the start of industrialization.

The depreciation structure in (5) is characterized by three parameters. It is assumed that a fraction φ_L of emitted carbon stays in the atmosphere forever, while a fraction $(1 - \varphi_0)$ of the remaining emissions exit into the biosphere. The remaining part decays at geometric rate φ . Thus,

$$1 - d_n = \varphi_L + (1 - \varphi_L)\varphi_0(1 - \varphi)^n. \quad (6)$$

The level of the GHG concentration can be then decomposed to a permanent part, Γ_t^p , and a decaying part, Γ_t^d :

$$\Gamma_t = \Gamma_t^p + \Gamma_t^d, \quad (7)$$

where

$$\Gamma_t^p = \Gamma_{t-1}^p + \varphi_L f_t, \quad (8)$$

$$\Gamma_t^d = (1 - \varphi)\Gamma_{t-1}^d + (1 - \varphi_L)\varphi_0 f_t. \quad (9)$$

Energy can be produced by using fossil or renewable sources. We will distinguish between substitutability in production versus substitutability in consumption between the two forms of energy. More precisely, we assume that energy derived from fossil fuel and that derived from renewable sources are perfect substitutes in the production of the final good.⁶ As we measure fossil fuel use in units of carbon content, the flow of anthropogenic GHG emissions equals f_t , the fossil fuel used in energy production in period t . Let ϖ_t denote the available stock of fossil fuel in period t . Given ϖ_0 , the law of motion for ϖ_t is

$$\varpi_{t+1} \leq \varpi_t - f_t. \quad (10)$$

We assume imperfect substitutability when capital is used in the production of different forms of energy. Fossil-fuel-derived energy production uses fossil fuel and capital as inputs according to production function

$$e_t^f \leq A_f (f_t)^{1-\alpha_f} (k_t^f)^{\alpha_f}, \quad (11)$$

where $A_f > 0$ and $\alpha_f \in (0, 1)$. This specification captures that, by using additional capital, more energy can be extracted from the remaining fossil fuel reserves.

We assume a competitive sector of renewable energy-producing firms. As these are heterogeneous, we will need to keep track of the identity, j , of each individual firm. The renewable energy output of firm j is given by

$$e_{j,t}^r \leq \Psi(i_{j,t}) (\mathcal{E}_{j,t})^{1-\alpha_r} (k_{j,t}^r)^{\alpha_r}, \quad (12)$$

where $\mathcal{E}_{j,t}$ is firm j 's productivity parameter, $\mathcal{E}_{j,0}$ is given, for all j , and $\alpha_r \in (0, 1)$. We interpret $i_{j,t}$ as the *new technology adoption rate* by firm j in period t . We wish to capture that the process of adopting new capital is costly and can result in temporary disruptions. One way to model this effect would be by explicitly introducing different vintages of clean capital, with older vintages scrapped and replaced by more productive new ones. This would naturally lead to a distribution of vintages within and across firms. To avoid the resulting technical complexity, and since distributional issues are not the focus of our study, we adopted a “reduced-form” approach to modeling this effect.⁷ While we will not explicitly account for vintages, we will model the costs associated with investment in new capital adoption by assuming that while it boosts future productivity, new capital adoption has a cost in terms of a contemporaneous output loss. More precisely, we assume that investment in new capital, i , reduces firm j 's current output by a factor $\Psi(i_{j,t}) \geq 0$, where $\Psi(\cdot)$ is such that $\Psi(0) = 1$,

⁶Hassler et al (2020) allow for imperfect output substitutability in energy and concentrate on medium-run questions.

⁷There is extensive literature on dynamic vintage-capital-related models. See, for example, Benhabib and Rustichini (1991), Chari and Hopenhayn (1991), Greenwood, Hercowitz, and Krusell (1997), and Jovanovic (2012). Boucekkine, De La Croix, and Licandro (2017) provide a recent review.

$\Psi'(\cdot) < 0$, $\Psi''(\cdot) < 0$, and $\Psi(\bar{i}) = 0$, for some \bar{i} . We interpret this as the total cost associated with the scrapping of “old” equipment.⁸

We will consider the possibility of a spillover effect, where aggregate technology adoption also affects the productivity of each individual firm. Put differently, as more firms adopt new technologies, the benefits affect the entire renewable energy sector. This creates an externality, leading to a discrepancy between equilibrium and desirable levels of new capital adoption. We consider this effect to be especially relevant, as investments in the energy sector tend to be capital intensive. Thus, if innovators do not expect to capture the resulting returns, under-adoption of new technologies relative to the optimum is likely to occur.⁹ More precisely, the productivity of firm j evolves according to

$$\ln \mathcal{E}_{j,t+1} \leq \xi i_{j,t} + (1 - \xi) \left(\int_0^1 i_{j,t} k_{j,t}^r dj / \int_0^1 k_{j,t}^r dj \right) + \ln \mathcal{E}_{j,t}, \quad (13)$$

where $0 \leq \xi \leq 1$ parametrizes the strength of the spillover effect. The case where $\xi = 1$ corresponds to no spillovers, while $\xi = 0$ corresponds to the other extreme, where productivity is entirely determined by spillovers. In order to abstract from any size-dependent advantage to firms, the above expression normalizes each firm’s technology adoption by its capital stock.

Each period, the production factors are allocated freely across sectors. Total capital used in the economy cannot exceed the total supply; i.e., for all t ,

$$k_t^c + k_t^f + \int_0^1 k_{j,t}^r dj \leq k_t. \quad (14)$$

In addition, the energy used in the production of the final good cannot exceed the total supply of energy:

$$e_t \leq e_t^f + \int_0^1 e_{j,t}^r dj. \quad (15)$$

The next section discusses desirable allocations for our model economy.

3 Efficiency

We begin by characterizing allocation efficiency in terms of some key relationships. We will later compare efficient outcomes to market allocations. The social

⁸Admittedly, important innovation also takes place in the fossil fuel sector. Mainly for simplicity, we will concentrate on technological progress in the renewable sector in our baseline model. We will later extend our model to account for technological progress in fossil fuel. This leads to some quantitative differences, but the qualitative features of our results will remain unchanged.

⁹Bosettia et al. (2008) argue that international knowledge spillovers tend to increase the incentive to free-ride, thus decreasing investments in energy R&D. Braun et al. (2009) perform an empirical study of spillovers in renewable energy. They document significant domestic and international knowledge spillovers in solar technology innovation, as well as significant international spillovers in wind.

planner chooses a sequence $\{c_t, k_t^c, k_t^f, f_t, e_t^f, \Gamma_t^p, \Gamma_t^d, \{i_{j,t+1}, k_{j,t}^r, \mathcal{E}_{j,t+1}, e_{j,t}^r\}_{j=0}^\infty, j \in [0, 1]$, to solve the following problem:

$$\max \sum_{t=0}^{\infty} \beta^t u(c_t)$$

subject to (8), (9), (10), (11), (12), (13), (14), (15) and

$$c_t + k_{t+1} \leq (1 - D_t(\Gamma_t^p + \Gamma_t^d)) \left[\tilde{A}_t (k_t^c)^{\theta_k} (l_t)^{\theta_l} (e_t)^{1-\theta} \right] + (1 - \delta)k_t, \quad (16)$$

as well as nonnegativity constraints and given the initial values for the stock variables.

We let μ_F denote the Lagrange multiplier on the production constraint in the fossil fuel sector (equation (11)), and μ_r^j be the multiplier on the production constraint for renewable energy firm j (equation (12)). Similarly, let $\mu_{\mathcal{E}}^j$ be the multiplier for the evolution of firm j 's productivity (equation (13)). Finally, μ_K and μ_E are the multipliers associated with the distribution of the capital stock across sectors, and with the supply of energy (equations (14) and (15)), respectively.

The first-order condition with respect to e_{jt}^r gives

$$\int_0^1 \mu_{r,t}^j dj = \mu_{E,t}. \quad (17)$$

Moreover, the marginal utility from producing an extra infinitesimal amount of renewable energy should be equal across firms; i.e.,

$$\mu_{r,t}^j = \mu_{r,t}^h, \text{ for any two firms } j \text{ and } h. \quad (18)$$

The first-order condition with respect to $k_{j,t}^r$ gives

$$(1 - \xi) \left(\frac{i_{j,t} - \bar{i}_t}{\bar{k}_t^r} \right) \int_0^1 \mu_{\mathcal{E},t}^j dj + \Psi(i_{j,t}) \alpha_r \mu_{r,t}^j \left(\frac{\mathcal{E}_{j,t}}{k_{j,t}^r} \right)^{1-\alpha_r} = \mu_{K,t}, \quad (19)$$

where $\bar{k}_t^r = \int_0^1 k_{j,t}^r dj$, and $\bar{i}_t = \int_0^1 i_{j,t} k_{j,t}^r dj / \int_0^1 k_{j,t}^r dj$. Since (17) and (18) give that $\mu_{r,t}^j = \mu_{E,t}$, equation (19) implies that the only non-aggregate variable that influences $i_{j,t}$ is $\frac{\mathcal{E}_{j,t}}{k_{j,t}^r}$.

The first order condition with respect to $i_{j,t}$ gives

$$-\mu_{r,t}^j \Psi'(i_{j,t}) \left(\frac{\mathcal{E}_{j,t}}{k_{j,t}^r} \right)^{1-\alpha_r} = \xi \frac{\mu_{\mathcal{E},t}^j}{k_{j,t}^r} + (1 - \xi) \frac{\int_0^1 \mu_{\mathcal{E},t}^j dj}{\bar{k}_t^r}. \quad (20)$$

Finally, the first-order condition with respect to e_t^f gives

$$\mu_{E,t} = \mu_{F,t}. \quad (21)$$

Since $\mu_{r,t}^j = \mu_{E,t} = \mu_{F,t}$, and $i_{j,t}$ is a function of $\frac{\mathcal{E}_{j,t}}{k_{j,t}^r}$, we have that $\frac{\mu_{\mathcal{E},t}^j}{k_{j,t}^r}$ is also a function of $\frac{\mathcal{E}_{j,t}}{k_{j,t}^r}$. The following result greatly simplifies our analysis. It asserts that if $\mathcal{E}_{j,t}$ and $k_{j,t}^r$ are proportional to the initial values of $\mathcal{E}_{j,0}$, then $i_{j,t} = i_t$, for all j and t . In other words, although renewable energy-producing firms are heterogeneous, efficiency implies that they choose identical levels of i_t .

Proposition 1 *In an efficient allocation, $\frac{k_{j,t}^r}{\mathcal{E}_{j,t}} = \frac{k_t^r}{\mathcal{E}_t}$ and $i_{j,t} = i_t$, for all j .*

Proof. For any initial values of $\mathcal{E}_{j,0}$, there is a solution such that $\mathcal{E}_{j,t}$, $k_{j,t}^r$, $\mu_{\mathcal{E},t}^j$, and $\mu_{r,t}^j$ are proportional to the initial values of $\mathcal{E}_{j,0}$. Then (20) implies that $i_{j,t} = i_t$, for all $j \in [0, 1]$. From (19), $\frac{\mathcal{E}_{j,t}}{k_{j,t}^r}$ is a function of $i_{j,t}$ only. As $i_{j,t} = i_t$, we have $\frac{\mathcal{E}_{j,t}}{k_{j,t}^r} = \frac{\mathcal{E}_t}{k_t^r}$. ■

4 Equilibrium and Optimal Policy

We derive the competitive equilibrium FOC for consumers and firms in the Appendix. Using these, we first characterize the equilibrium choice of investment in the renewable technology. In what follows, we let $\Phi_t(i_{j,t})$ stand for the government policy conditional on a renewable firm's investment. Provided that $\xi < 1$, in the absence of government policy this investment will be lower than optimal. Of course, the magnitude of the distortion depends on the level of the externality, ξ .

Proposition 2 *In a competitive equilibrium with $\Phi_t(i_{j,t}) = 0$, $i_{j,t}$ is lower than optimal when $\xi < 1$.*

The proof is given in the Appendix. Next, we discuss optimal policy. This needs to take into account two distortions. First, there is under-investment in i_t , due to the spillover effects. The second distortion is due to the social costs associated with the environmental externality from GHG emissions. The next Proposition demonstrates that both distortions can be fully accommodated through the use of two instruments. First, a policy that taxes firms in proportion to their under-investment in i_t restores optimal investment by making firms indifferent between paying a “penalty” or pursuing the optimal level of investment. Second, a Pigouvian tax internalizes the externality from carbon emissions. As in GHKT (2014), under the special assumptions of log utility and 100% depreciation of capital, the Pigouvian tax imposed on the fossil fuel firms does not depend on the growth rate of the economy.

Proposition 3 (1) *The optimal allocation can be supported by a combination of a revenue-neutral policy, $\Phi_t^j(i_{j,t}) = -(1 - \xi)p_t^e \Psi'(i_t^*) \left(\frac{e_{j,t}^{*r}}{\Psi(i_{j,t}^*)} \right) (i_{j,t} - i_t^*)$, imposed on renewable firms, together with a Pigouvian tax on fossil fuel use, $\tau_t^f = \sum_{j=0}^{\infty} \beta^j \frac{u'(c_{t+j}^*)}{u'(c_t^*)} \pi_{t+j} y_{t+j}^* (1 - d_j)$, where p_t^e is the price of energy, $\{c_t^*, y_t^*, i_t^*\}_{t=0}^{\infty}$*

is the solution to the planner's problem, and $1 - d_j = \varphi_L + (1 - \varphi_L)\varphi_0(1 - \varphi)^j$. (2) If $u(c) = \log(c)$, $\alpha_r = \alpha_f = \alpha$, $\pi_t = \pi$, all t , and $\delta = 1$, $\tau_t^f = y_t \pi \left[\frac{\varphi_L}{1-\beta} + \frac{(1-\varphi_L)\varphi_0}{1-(1-\varphi)\beta} \right]$ does not depend on the growth rate of the economy.

The proof is given in the Appendix. The optimal policy in our model has several interesting implications. First, the policy on renewable energy firms generates no revenue, but it reduces the household's profits from the renewable sector, as a result of inducing additional innovation compared to the competitive equilibrium. Second, the Pigouvian tax reduces the household's profits from the fossil fuel sector. However, the household receives a lump-sum transfer of equal magnitude; thus, its budget constraint remains unchanged. Finally, there is a separation between the two schemes, as the total effect on the household's budget is the same as the resource cost of innovation in the planner's problem.

For the remainder of the paper we will assume that $u(c) = \log(c)$ and will set $\delta = 1$. Moreover, we will assume that the stock of fossil fuel is large enough so that consumption of fossil fuel is not constrained. In the Appendix we solve the planner's problem backward, from a final state, where only renewable energy is used, and show that the consumption of fossil fuel is endogenously bounded. In other words, the full transition to the renewable energy regime takes place prior to the exhaustion of fossil fuel resources. This is due to the growing productivity in the renewable sector eventually surpassing a threshold that makes using fossil fuel the less efficient source. While allocating additional capital to the fossil fuel sector increases the production of energy per unit of fossil fuel, the present value of the marginal environmental damages limits the overall benefit from fossil fuel use. In the next section we calibrate our model in order to study the optimal timing of the transition to a renewable energy regime, as well as the effects of the GHG accumulation prior to this transition. This will allow us to explore the quantitative significance of the scrapping effect on optimal policy and welfare.

5 Calibration

In this section we calibrate our model in order to study the transition from the current, predominantly fossil fuel economy, to an economy that fully relies on renewable energy. We use the calibrated model to evaluate the interaction between the two policy instruments: (i) the Pigouvian taxation on carbon emissions, and (ii) the technology adoption targeting for renewable energy firms. More precisely, we evaluate how the two policies would affect the share of renewable energy, the accumulation of GHG, global temperatures, economic growth, and welfare, first in isolation, and then in tandem. This will allow us to quantify the significance of the scrapping effect and to explore the potential substitutability between the two policy tools.

The model's parameters can be divided into four categories related to preferences, technology, environmental damages, and the current (status quo) policies in place. We will use a log utility function and a benchmark annual discount

rate of 4%, which gives $\beta = 0.96^{10}$, as a period is calibrated to 10 years.¹⁰ Given the length of the period, there is some justification in considering the benchmark case of full depreciation of capital, $\delta = 1$. Turning to the aggregate Cobb-Douglas production function, we set the share of capital and labor, respectively, to $\theta_k = (1/3) \times 0.95$ and $\theta_l = (2/3) \times 0.95$, which imply an energy share of $1 - \theta = 1 - (\theta_k + \theta_l) = 0.05$. We set the productivity growth rate in the final good sector so that the balanced growth rate is 2%, while the long-run population growth rate is set to zero.

We assume the following form for the renewable technology adoption cost function, Ψ :

$$\Psi(i) = \left(1 - \left(\frac{i}{\bar{i}} \right)^\psi \right)^{1/\psi}.$$

This functional form satisfies the earlier assumptions that $\Psi(0) = 1$, $\Psi'(\cdot) < 0$, $\Psi''(\cdot) < 0$, and $\Psi(i) = 0$, for $i = \bar{i}$. Moreover, the elasticity of the technology adoption cost with respect to the adoption rate is given by

$$-\frac{\Psi'(i)}{\Psi(i)} = \frac{1}{i} \times \frac{(i/\bar{i})^\psi}{1 - (i/\bar{i})^\psi}. \quad (22)$$

As shown in the Appendix, this elasticity plays an important role in determining both the long-run and the transitional technology adoption rate in the renewable sector. The parameter ψ provides us with a degree of freedom to match a long-run adoption rate that is consistent with the long-run growth rate of the economy. To calibrate Ψ , we need to assign values to two parameters: \bar{i} (the highest possible technology adoption rate in the renewable sector) and ψ . We will use the relationship between $\Psi(\cdot)$ and the optimal asymptotic long-run growth rate of i^l , the productivity in the renewable sector. As we show in the Appendix, if the spillover externality is fully internalized, the long-run i^l is given by

$$-\frac{\Psi'(i^l)}{\Psi(i^l)} = \frac{\beta}{1 - \beta} (1 - \alpha).$$

Combining the above equation with (22) gives:

$$\bar{i} = \left(1 + \frac{1}{\left(\frac{\beta}{(1-\beta)} (1 - \alpha) i^l \right)} \right)^{1/\psi} \times i^l. \quad (23)$$

Thus, for a given i^l , a lower ψ implies a higher \bar{i} . In our baseline calibration, we set \bar{i} to its maximum attainable level, which corresponds to setting ψ to its lowest possible level; i.e., by setting $\psi = 1/(1 - \alpha) = 2$.¹¹

¹⁰Most macroeconomic studies use yearly discount rates between 2% and 5%.

¹¹If $\psi = 1/(1 - \alpha) < 2$, then $\Psi(i)^{\frac{1}{1-\alpha}}$ is no longer a concave function and the cost of technological adoption is no longer increasing.

To determine i^l , note that an asymptotically balanced growth path requires equal asymptotic growth rates between the renewable energy sector (which is the only source of energy in the long-run) and the final good sector. This, in turn, implies $i^l = \log\left(g^l \times (g^c)^{\frac{1}{\bar{i}}}\right) = 0.198$. Using (23), we set $\bar{i} = 0.489$.¹²

We follow GHKT (2014) in our calibration of the environmental damage parameters and the computation of the Pigouvian carbon tax. In particular, we set $\pi = 2.379 \times 10^{-5} \times 10$, $\varphi = 0.0228$, $\varphi_L = 0.2$, and $\varphi_0 = 0.393$. The optimal carbon tax follows from the last part of (83) in the Appendix and is given by

$$\mathcal{T}_P/y = \pi \left[\frac{\beta\varphi_L}{(1-\beta)} + \frac{(1-\varphi_L)\varphi_0}{(1-\beta(1-\varphi))} \right]. \quad (24)$$

Given our calibration, this equation implies that $\mathcal{T}_P/y = 3.55 \times 10^{-4}$, which is equivalent to a tax of \$24.9 per ton. This is broadly consistent with the climate economics literature given the assumed level of discounting.

We chose 2015 as our base year. Four parameters related to the energy sector remain to be calibrated: the current stock of fossil fuel, W_0 , the current productivity of the renewable sector, \mathcal{E}_0 , the current Pigouvian tax level, τ^f , and the spillover from the renewable technology adoption, ξ . For our baseline calibration we set $W_0 = 666GtC$.¹³

We set \mathcal{E}_0 , τ^f , and ξ to match three data moments: (i) the current share of renewable energy in total energy production, s_0 , (ii) the current consumption of fossil fuel, f_0 , and (iii) the change in the share of renewable energy in the last period (10 years), $s_0 - s_{-1}$. The current productivity of the renewable sector affects the renewable share in total energy production. In turn, the spillovers from the renewable technology adoption affect the change in the productivity of the renewable sector, and thus the change in the share of renewable energy. In addition, the Pigouvian tax affects the use of fossil fuel and, consequently, the share of fossil fuel and renewable sources in total energy production. In what follows, we denote by τ^f the value of the Pigouvian tax as a percentage of its optimal level, τ^* . Setting $\mathcal{E}_0 = 14.92$, $\tau^f = 0.63 \cdot \tau^*$, and $\xi = 0.54 \cdot \xi^*$, our model matches $f_0 = 100 GtC$,¹⁴ $s_0 = 10.2\%$, and $s_0 - s_{-1} = 2.3\%$.¹⁵

¹²For sensitivity, we also set \bar{i} to levels corresponding to 10 and 20 percent slower than the maximum attainable renewable technology growth rate. These slower rates correspond to setting \bar{i} to 0.449 and 0.408, respectively. These translate to a maximum attainable annual growth rates of 4.6 and 4.2 percent, respectively, instead of the 5.0 percent baseline. In our robustness exercise we will accordingly set ψ equal to 2.21 and 2.50, respectively, in order for \bar{i} to satisfy (23).

¹³See Section 4.3 in Li, Narajabad, and Temzelides (2016).

¹⁴See EPA: <https://www.epa.gov/ghgemissions/global-greenhouse-gas-emissions-data#Trends>.

¹⁵This includes all modern plus traditional renewables (including biomass). We calculated an initial 10-year growth rate of 4.7% for renewables, with a corresponding rate of 2% for the entire energy sector (we excluded nuclear energy from this calculation). See <https://www.ren21.net/reports/global-status-report/>. We remark that while, with a few exceptions, an explicit carbon tax is largely absent in most countries, several uses of fossil fuel are taxed at relatively high rates. Gasoline and other fuel related to transportation are a leading example. The initial value of τ^f should be interpreted in that light, as the difference

6 Quantitative Findings

Our calibration allows us to evaluate the quantitative significance of the scrapping effect, as well as the effects of the carbon tax and the renewable adoption policy in isolation and in tandem. We simulate our model considering different scenarios for the two policy parameters. Figure 1 below shows the paths for the share of renewable energy (top), accumulated fossil fuel consumption (middle), and global temperatures (bottom), in each respective policy scenario. The dotted, dashed, dot-dashed, and solid lines indicate the status quo benchmark (business as usual), optimal technology adoption, optimal Pigouvian tax, and combined optimal policies (full optimum), respectively. Clearly, the outcomes under either an optimal Pigouvian tax policy alone or the optimal technology adoption policy alone differ significantly from the outcome when both policies are present. This thought-experiment helps us understand how the two policies interact in the presence of the scrapping channel. Next, we comment on each panel individually.

The first panel gives the share of renewables in energy production as a function of time under the different policy scenarios. Note that the optimal technology adoption policy leads to a "rotation" of the status quo path, while the Pigouvian tax "shifts" the status quo path along the transition. As a result, setting technology adoption to its optimal level in the absence of the optimal Pigouvian tax *reduces* the share of renewables in the short run relative to the status quo. At the same time, the full switch to renewable energy production occurs somewhat earlier than in the benchmark case. In contrast, setting the Pigouvian tax to its optimal level in the absence of a policy inducing optimal technology adoption increases the share of renewable energy immediately. In the full optimum, setting both policies to their combined optimal levels reduces the short-run share of renewable energy. However, the transition to a fully renewable global economy takes place by 2070, the earliest among the four scenarios.¹⁶

The second panel describes the evolution of cumulative fossil fuel consumption in the same four scenarios. Interestingly, absent a tax on GHG emissions, the cumulative fossil fuel consumption is initially somewhat more intense if the technology externality is internalized than in the status quo. This is because the faster growth in renewable energy productivity allows the economy to rely fully on renewable energy earlier. Similarly, when both the Pigouvian tax and the technology adoption are set to their optimal level the economy reaches the fully renewable energy state earlier and more fossil fuel is left unused. Consistent with the "green paradox," this also implies a heavier use of fossil fuel initially than in the case where the Pigouvian tax is in place but the renewable policy is

between the marginal cost to fossil fuel producers and the average price paid by consumers of fossil fuel. Of course, the fossil fuel market shares many characteristics of an oligopoly.

¹⁶Note that the fossil fuel consumption drops to zero in finite time, not just asymptotically. The reason for this is that fossil fuel and renewable energy are assumed to be perfect substitutes in consumption. Thus, as the consumption of fossil fuel vanishes, its marginal productivity, which depends on the marginal productivity of energy, remains finite. Since damages from emissions grow proportionally to GDP, there is a point after which the productivity of renewables becomes high enough to make fossil fuel obsolete.

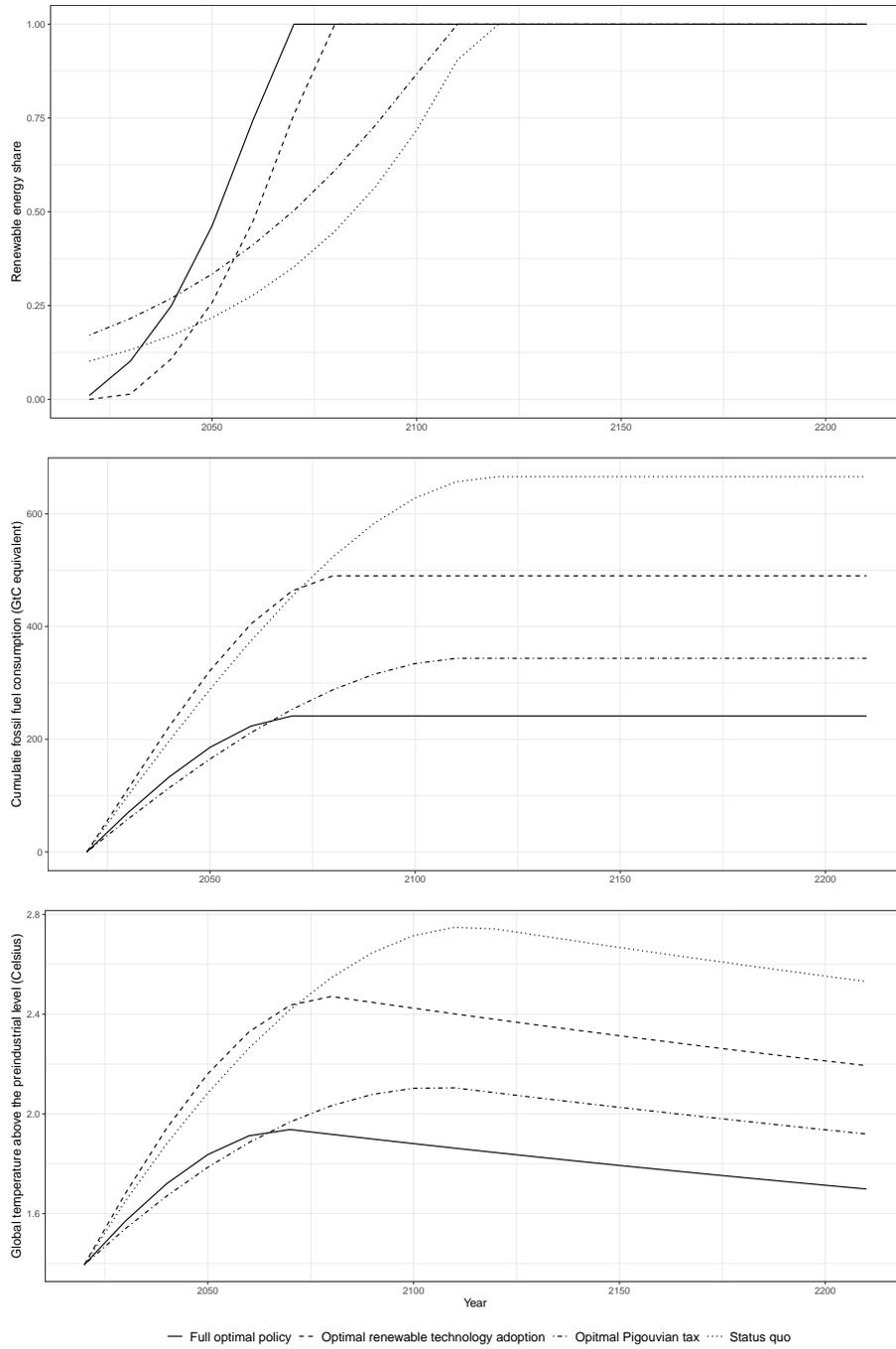


Figure 1: Benchmark calibration: Energy and Temperature

absent. By comparison, GHKT (2014) find that, while increasing in the status quo, optimal consumption of fossil fuel stays relatively flat.

The third panel shows the path for global temperatures under our four policy scenarios. In order to map carbon concentrations into global temperatures, T , we use the following expression (see GHKT, 2014):

$$T(S_t) = 3 \ln \left(\frac{S_t}{\bar{S}} \right) / \ln(2),$$

where \bar{S} is the pre-industrial level of atmospheric carbon concentration. Consistent with the fossil fuel use in the top panel, the global temperature increases under both the business-as-usual and the optimal technology adoption scenario, reaching short of 2.8 degrees Celsius above the pre-industrial level. The temperature under the technology policy alone (in the absence of a Pigouvian tax) later falls slightly faster than in the benchmark case. Under the optimal Pigouvian tax and in the fully optimal case, global temperatures peak at around 2.2 and 2.0 degrees Celsius above the pre-industrial level, respectively, and then decline over time. Mainly due to a higher assumed total endowment of fossil fuel, GHKT (2014) find a peak temperature of almost 10 degrees Celsius above the pre-industrial level without policy intervention. The optimal tax limits heating to about 3 degrees Celsius in their model.

The three panels in Figure 2 describe the over-time contribution of certain key variables to related growth rates under our four policy scenarios. The top panel shows the period-by-period difference in related damages caused by GHG emissions. Of note, the implementation of the technology policy in the absence of a carbon tax has a greater negative effect on growth compared to the status quo. After the full transition takes place, the contribution to growth is positive (if small) in all four cases, due to the gradual decline in the stock of emissions. The second panel plots the contribution of the energy sector to economic growth. The status quo scenario results in a sizable negative contribution to growth. This is partly due to damages and partly due to scarcity and the resulting increase in the shadow price of fossil fuel. As the resource constraint on fossil fuel is far from binding under the fully optimal policy scenario, equation (85) in the Appendix implies that the net contribution of energy to growth is positive and increasing during the energy transition.

Next, we turn our attention to welfare comparisons across these scenarios. Following Lucas (1987), we report the consumption-equivalent percentage welfare gain from these policies over the business-as-usual benchmark. Moving from the status quo to optimal technology adoption alone (in the absence of a Pigouvian tax) would imply a 0.251% consumption-equivalent gain, while the optimal Pigouvian tax alone would result in a gain of 1.023%, confirming the relative importance of the carbon tax. Comparing the status quo to the scenario where both policies are implemented results in a consumption-equivalent welfare gain of 1.431%. This is one of the main findings of our quantitative analysis. The difference between the welfare gain from applying either policy in isolation versus implementing both amounts to about 0.157% increase in consumption,

suggesting a sizeable complementary between the two policies. Thus, our model points to sizable welfare gains only when the policies are adopted in tandem.

To further highlight the role of the scrapping channel in these findings, we run the model under the same parametrization as before, but with the scrapping costs “shut down;” i.e., $\Psi = 1$. In the absence of scrapping, we set the growth rate in the renewable technology equal to its long-run value, as implied by the balanced growth path. We then target $f_0 = 100 \text{ GtC}$, which implies $s_0 - s_{-1} = 2.1\%$. The resulting Pigouvian tax rate is close to the one under scrapping: $\tau^f = 0.62 \cdot \tau^*$. The implied dynamics for the share of renewables, fossil fuel consumption, and global temperature, as well as the corresponding effects on growth, are reported in Figures 3 and 4. By comparing to the case with scrapping, we notice a number of important differences. Optimal penetration by renewables starts lower in the case with scrapping, but it soon overtakes, and the transition to the fully renewable state occurs earlier in this case. Fossil fuel consumption and global temperatures demonstrate corresponding differences. In the case without scrapping, the consumption-equivalent welfare gain from setting the Pigouvian tax to its optimal level (fully optimal policy) corresponds to an 1.05% increase in consumption. We conclude that the scrapping channel plays a significant role when we quantify the optimal energy transition, as the difference between the welfare gain from applying the fully optimal policy with versus without scrapping amounts to an approximate 0.381% increase in consumption.

6.1 Productivity growth in the fossil fuel sector

As a robustness check, here we explore how are findings are affected if we consider productivity growth in the fossil fuel sector. We calibrate this to grow at the same rate as it did between 1950 and 2000. We make two additional assumptions. First, we assume a constant share of energy in the global economy during these five decades. Second, we assume that renewable energy was a small share of total energy, and that almost the entire increase in energy production during that period was due to the rise in the use of fossil fuel. Between 1950 and 2000, the annualized growth rate of world GDP in constant prices was 1.68 percent. In the same period, the annualized growth rate of CO2 emissions was 1.27 percent.¹⁷ Based on these observations, and assuming a constant carbon intensity, the productivity of the fossil fuel sector has grown at the annualized rate of 0.40 percent during that period.

Incorporating productivity growth in fossil fuel changes the calibrated values of both the spillover parameter, ξ , and the Pigouvian tax rate, τ^f , relative to the benchmark calibration. The biggest difference is in the new calibrated value of ξ , which is closer to the optimal level at $\xi = 0.69 \cdot \xi^*$ compared to $\xi = 0.54 \cdot \xi^*$ in the benchmark calibration. This is because the renewable sector must now exhibit higher productivity growth relative to the benchmark in order to match

¹⁷See <https://www.statista.com/statistics/264699/worldwide-co2-emissions/> and <https://ourworldindata.org/grapher/world-gdp-over-the-last-two-millennia>.

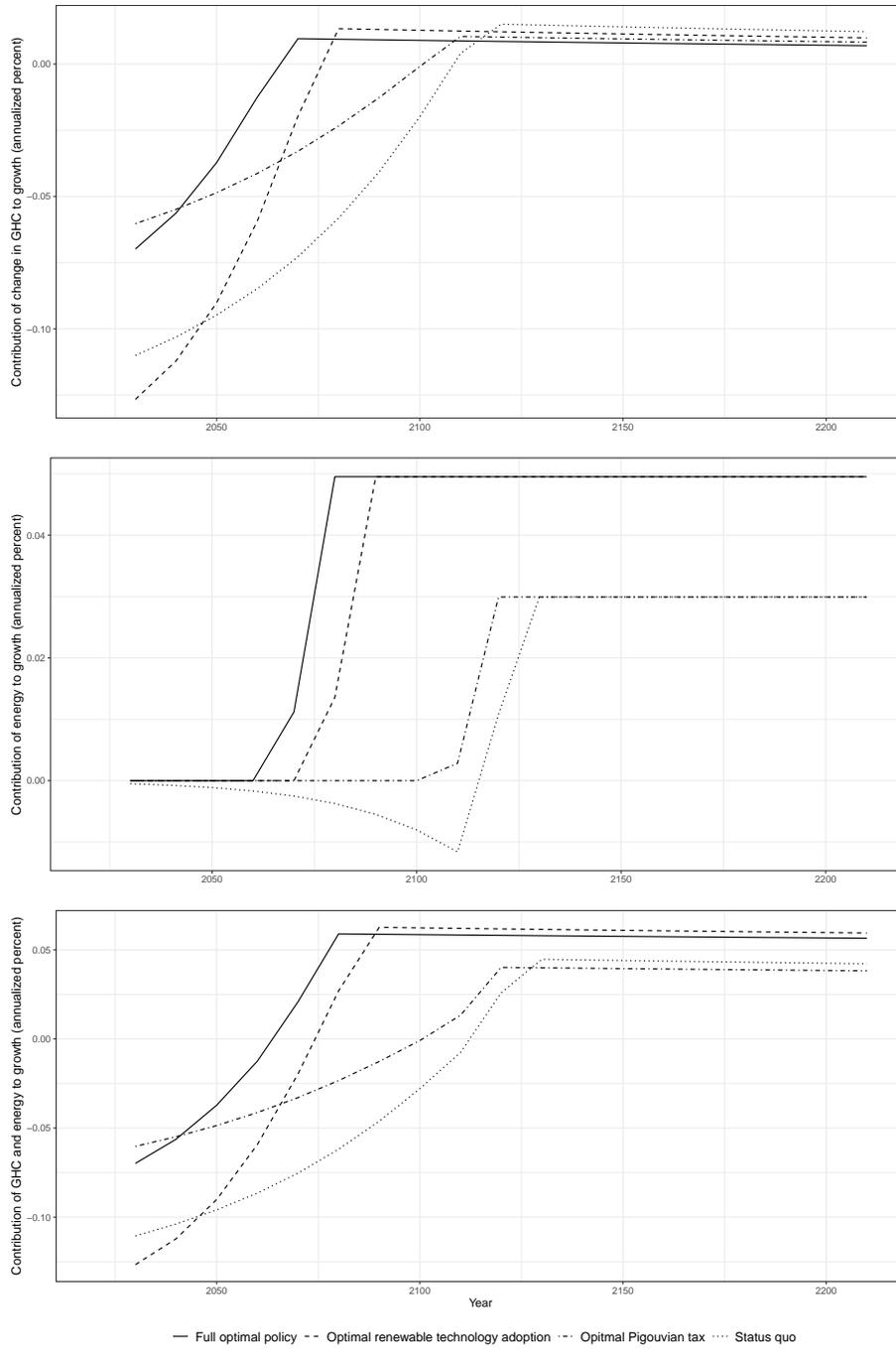


Figure 2: Benchmark calibration: Growth contributions

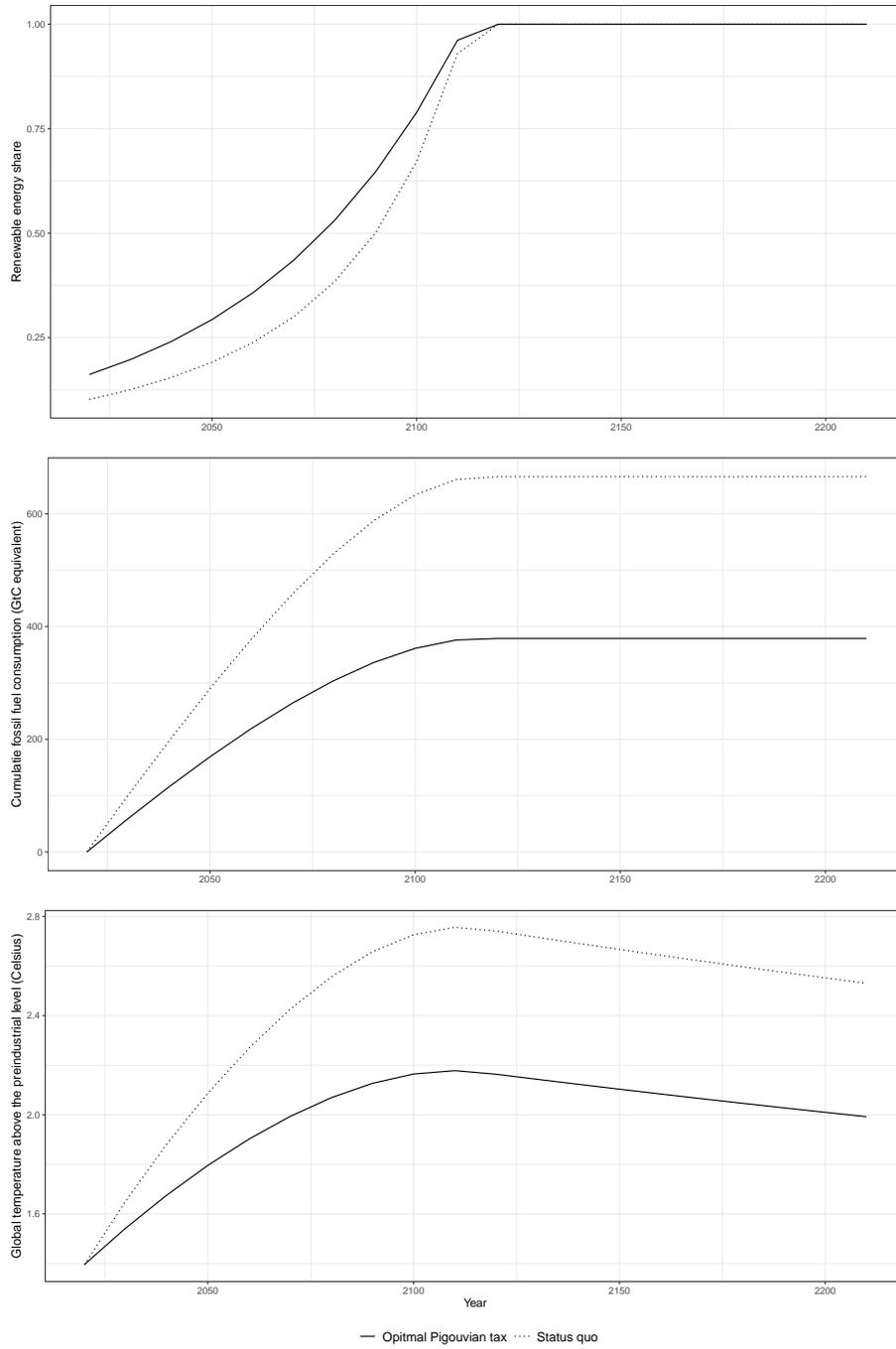


Figure 3: No scrapping: Energy and Temperature

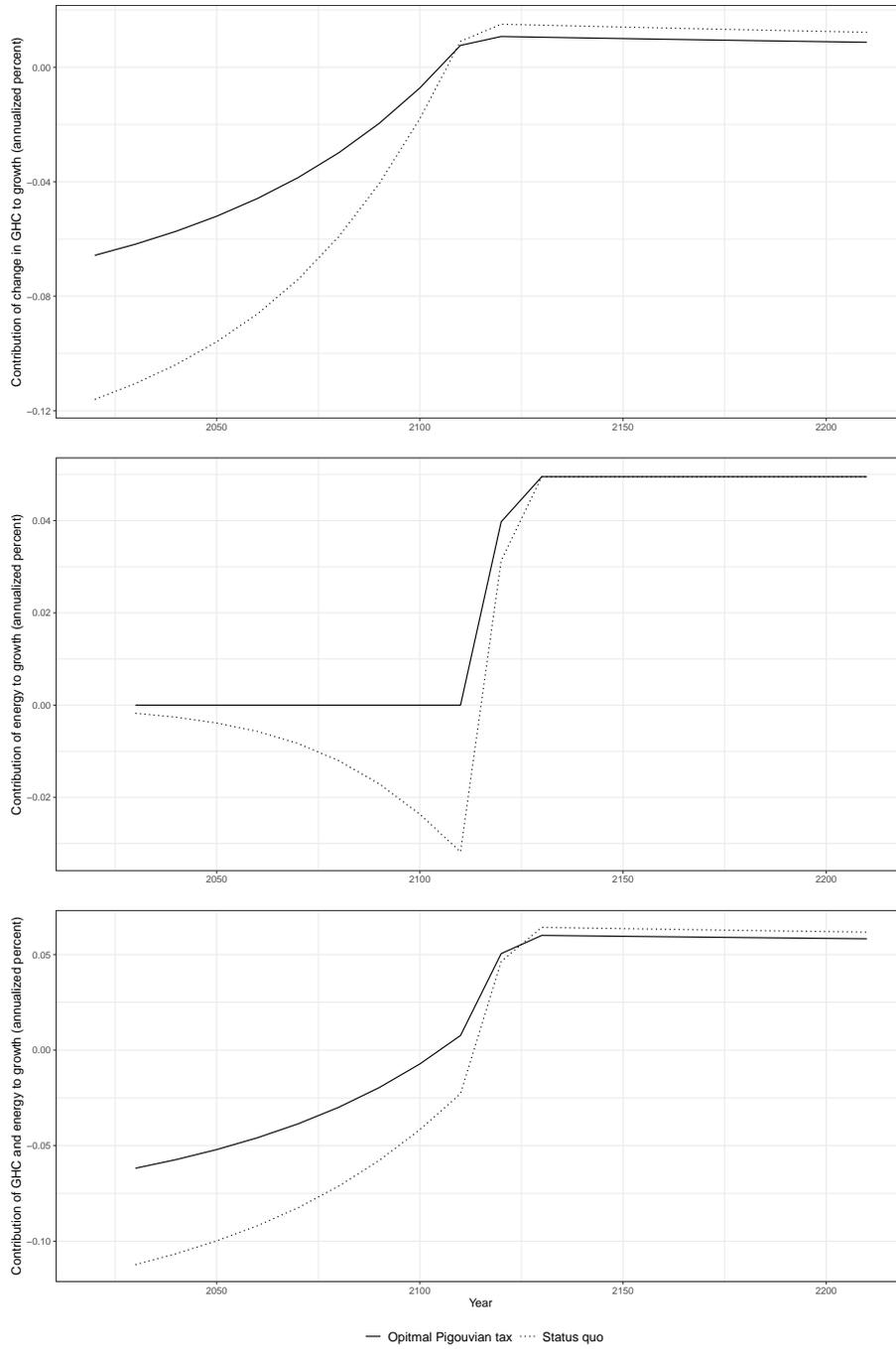


Figure 4: No scrapping: Growth contribution

the same level of increase in the share of renewables. In contrast, the calibrated value for the Pigouvian tax rate remains at $\tau^f = 0.63 \cdot \tau^*$, almost the same as its benchmark calibrated level.

Figure 5 shows the paths for the share of renewable energy (top), accumulated fossil fuel consumption (middle), and global temperatures (bottom), under our four scenarios. Like in Figure 1 previously, these scenarios correspond to the status quo (dotted line), optimal renewable technology adoption (dashed line), optimal Pigouvian carbon taxation (dot-dashed line), and combined optimal policies (solid line).

A comparison between Figures 1 and 5 reveals that the economy reaches the full renewable stage earlier when we incorporate productivity growth in the fossil fuel sector to the model. This seemingly counter-intuitive result is due to the difference in the calibrated value of ξ , as the spillover from renewable technology adoption is higher when there we incorporate productivity growth in fossil fuel. As a result, the productivity of the renewable sector grows faster and surpasses the level at which the fossil fuel sector is no longer competitive earlier. In addition, as the middle panel of Figure 5 demonstrates, fossil fuel is not exhausted under the status quo path. Consequently, the maximum global temperature reaches 2.6 degree Celsius above the pre-industrial level under the status quo (Figure 5 bottom panel), below the 2.8 degree Celsius achieved under the status quo path of the benchmark calibration (Figure 1).

The qualitative effects of switching from the status quo to the paths associated with optimal renewable technology adoption and optimal Pigouvian taxation, respectively, are similar to those in our benchmark calibration. As seen in the top panel of Figure 5, the optimal renewable technology adoption path results in an immediate lower renewable share. However, faster growth in the renewable sector results in an earlier transition to a fully renewable economy. In contrast, switching from the status quo to the optimal Pigouvian taxation path would result in an immediate rise in the renewable share, but the path for renewables in this case is more or less parallel to the status quo. Finally, The combined optimal policy leaves the current level of renewable energy share more or less unchanged, but the resulting path in this case would be parallel to the optional adoption path, thus reaching the fully renewable economy faster than in the other cases. The paths for fossil fuel consumption and for global temperatures (middle and bottom panels of Figure 5) remain similar to those in the benchmark calibration (middle and bottom panels of Figure 1).

Moving from the status quo to optimal technology adoption alone (but no Pigouvian tax) would imply a 0.74% consumption-equivalent gain, while the optimal Pigouvian tax alone would result in a gain of 1.09%, confirming the relative importance of the carbon tax. Comparing the status quo to the situation where both policies are applied results in a consumption-equivalent welfare gain of 1.53%. These findings are broadly consistent with the welfare gains in our benchmark case.

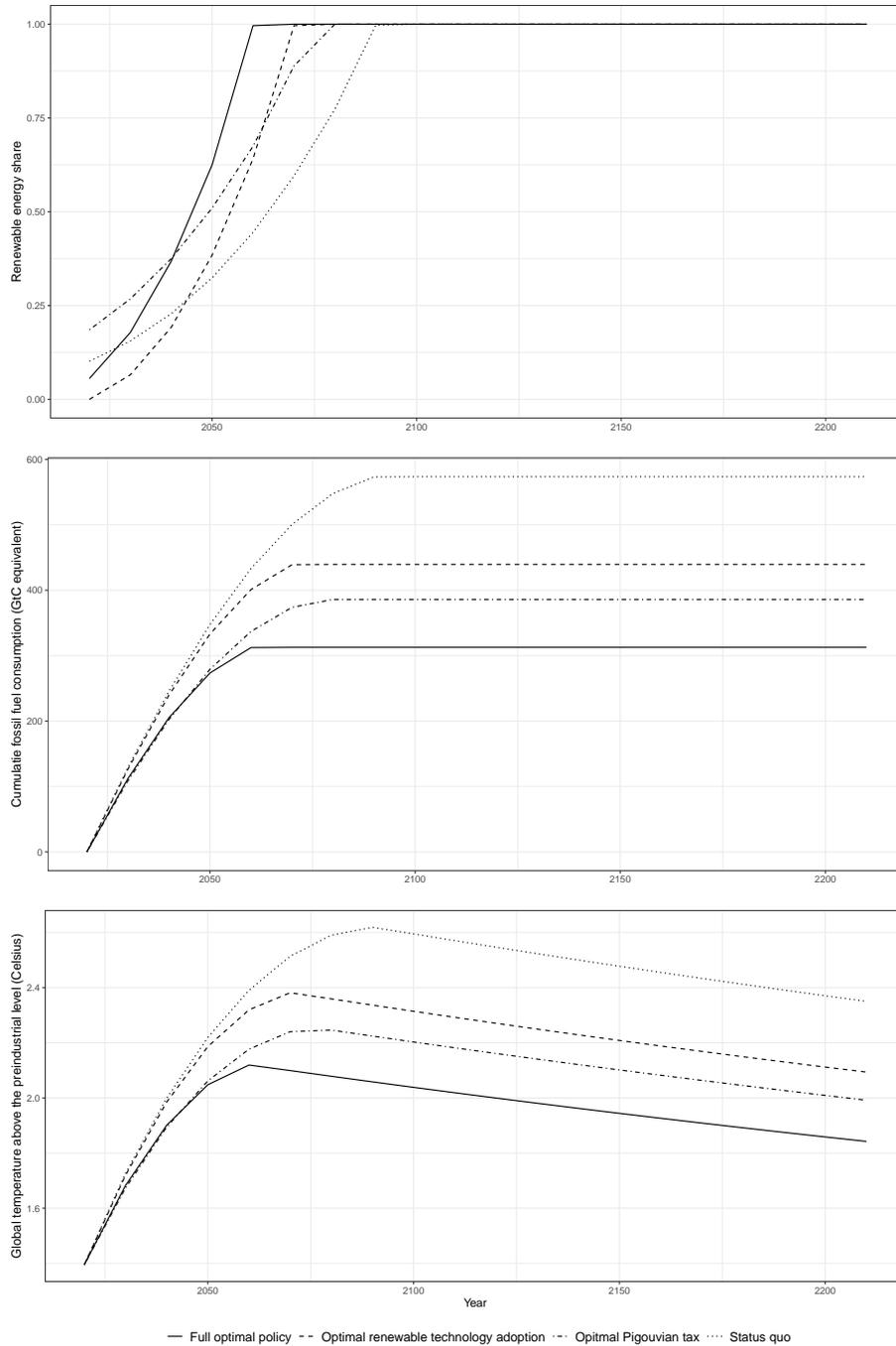


Figure 5: Long-run economy with productivity growth in the fossil fuel sector

7 Conclusion

We incorporated scrapping costs associated with adopting new capital in the renewable energy sector in an IAM framework. As renewable technologies are still relatively new, such advancements can be frequent, resulting in significant costs. We showed that in a capital intensive industry like the energy sector, when technological progress is embedded in the capital stock, such costs can have sizable quantitative implications for the optimal share of renewable energy, especially in the short-run. We investigated their quantitative implications for the optimal energy transition. In the case where Pigouvian carbon taxes are infeasible, tax/subsidy policies that subsidize renewables, in our case by internalizing spillover effects, might not be a suitable substitute. Hassler et al. (2020) found that, when it comes to accomplishing climate-related goals, making renewable energy cheaper is not an effective substitute for making fossil fuel more expensive. Our model reaches a similar conclusion. It suggests that these two policies are better thought of as complements. The tax/subsidy scheme forces firms to scrap a larger portion of their capital than under the status quo path. Particularly in early years, when the policy has not yet altered the productivity of the renewable sector relative to status quo, this discourages heavy investment in renewable energy capital. As time passes, and the policy results in a significantly more productive renewable sector, it becomes more profitable to invest in renewables, resulting in their share surpassing that of fossil fuel faster. This conclusion holds true when we incorporate technological progress in fossil fuel into the model.

8 Appendix

8.1 Optimization by Households and Firms

The representative household owns the firms, as well as the capital and fossil fuel stocks. It rents capital to firms and sells fossil fuel to the non-renewable sector. The representative household's problem is given by

$$\begin{aligned} & \max \sum_{t=0}^{\infty} \beta^t u(c_t) \\ & \text{s.t.} \\ & \sum_{t=0}^{\infty} p_t [c_t + k_{t+1} - (1 - \delta)k_t] \leq \\ & \sum_{t=0}^{\infty} p_t \left[r_t k_t + w_t l_t + p_t^f f_t + \int_0^1 \pi_{j,t}^r dj + z_t \right], \\ & \varpi_{t+1} \leq \varpi_t - f_t, \end{aligned} \tag{25}$$

where p_t is the Arrow-Debreu price of the period t final good, δ is the depreciation rate of capital, r_t is the rental price of capital, w_t is the wage rate, p_t^f is the price of fossil fuel, $\int_0^1 \pi_{j,t}^r dj$ stands for the profits of renewable firms, and z_t are lump-sum transfers from the government. The government collects taxes from the fossil fuel energy sector and rebates them lump-sum to households, balancing its budget in every period.

The first order conditions, which are also sufficient for a maximum, imply:

$$1 - \delta + r_{t+1} = \frac{\beta u'(c_{t+1})}{u'(c_t)}, \tag{26}$$

and

$$\frac{\beta u'(c_{t+1})}{u'(c_t)} = \frac{p_{t+1}}{p_t}. \tag{27}$$

Equation (26) says that the rental price of capital plus the non-depreciated part of capital must equal the marginal rate of substitution between consumption in two consecutive periods. Equation (27) says that the marginal rate of substitution between consumption in period t and consumption in period $t + 1$ must equal the relative price of the respective consumption goods.

The final good-producing firms rent capital, hire labor and buy energy in competitive markets, at prices w_t , r_t , and p_t^e , respectively. The representative firm in the final good sector solves:

$$\max \left[A_t \cdot (k_t^c)^{\theta_k} (l_t)^{\theta_l} (e_t)^{1-\theta} - r_t k_t^c - w_t l_t - p_t^e e_t \right].$$

The first-order conditions imply that the marginal input productivities equal their respective prices:

$$\theta_k A_t (k_t^c)^{\theta_k - 1} (l_t)^{\theta_l} (e_t)^{1-\theta} = r_t, \tag{28}$$

$$\theta_l A_t (k_t^c)^{\theta_k} (l_t)^{\theta_l - 1} (e_t)^{1 - \theta} = w_t, \quad (29)$$

and

$$(1 - \theta) A_t \frac{(k_t^c)^{\theta_k} (l_t)^{\theta_l}}{e_t^\theta} = p_t^e. \quad (30)$$

Firms in the fossil fuel sector rent capital and buy fossil fuel. Additionally, they pay a per unit tax on the GHG emission from fossil fuel use, τ_t . The representative firm in this sector solves:

$$\max \left[p_t^e A_f (f_t)^{1 - \alpha_f} (k_t^f)^{\alpha_f} - r_t k_t^f - (p_t^f + \tau_t) f_t \right].$$

The first-order conditions imply that the value of the marginal input productivities equal their respective prices:

$$p_t^e \alpha_f A_f \left(\frac{f_t}{k_t^f} \right)^{1 - \alpha_f} = r_t, \quad (31)$$

and

$$p_t^e (1 - \alpha_f) A_f \left(\frac{k_t^f}{f_t} \right)^{\alpha_f} = (p_t^f + \tau_t). \quad (32)$$

The production function for the renewable energy firms is given by (12). It depends on the firm's productivity, the firm's technology adoption rate, and the capital used. The firms in this sector rent capital and receive a subsidy, $\Phi(i_{j,t})$, which is a function of the firm's technology adoption rate, $i_{j,t}$. We allow $\Phi(i_{j,t})$ to be negative and assume it is differentiable. In each period t , the renewable firm j maximizes future discounted profits subject to (13):

$$\begin{aligned} \max \sum_{\tau=0}^{\infty} \beta^{t+\tau} u'(c_{t+\tau}) & \left[p_{t+\tau}^e \Psi(i_{j,t+\tau}) (\mathcal{E}_{j,t+\tau})^{1 - \alpha_r} (k_{j,t+\tau}^r)^{\alpha_r} - r_{t+\tau} k_{j,t+\tau}^r + \Phi(i_{j,t+\tau}) \right] \\ \text{s.t. } \ln \mathcal{E}_{t+1}^j & \leq \ln \mathcal{E}_t^j + \xi i_{j,t} + (1 - \xi) \left(\int_0^1 i_{j,t} k_{j,t}^r dj / \int_0^1 k_{j,t}^r dj \right) \\ & i_{j,t} \geq 0, \text{ and } \mathcal{E}_0 \text{ given.} \end{aligned} \quad (33)$$

Let $\lambda_{\mathcal{E},t}^j$ be the Lagrangian multiplier associated with equation (13). The first-order conditions of this problem are

$$p_t^e \alpha_r \Psi(i_{j,t}) \left(\frac{\mathcal{E}_{j,t}}{k_{j,t}^r} \right)^{1 - \alpha_r} = r_t, \quad (34)$$

$$-\beta^t u'(c_t) \left[p_t^e \Psi'(i_{j,t}) (\mathcal{E}_{j,t})^{1 - \alpha_r} (k_{j,t}^r)^{\alpha_r} + \Phi'(i_{j,t}) \right] = \xi \lambda_{\mathcal{E},t}^j, \quad (35)$$

and

$$\lambda_{\mathcal{E},t+1}^j + \beta^{t+1} u'(c_{t+1}) p_{t+1}^e (1 - \alpha_r) e_{j,t+1}^r = \lambda_{\mathcal{E},t}^j. \quad (36)$$

Equation (34) says that the value of the marginal productivity of capital should be equal to its rental price. Equation (35) says that the cost of increasing the adoption rate, which is the loss in production plus the marginal subsidy, should equal the benefit from increasing the adoption rate, which comes from the value of having a higher level of productivity next period. Equation (36) says that the value this period from relaxing constraint (13) should be equal to the value from relaxing that constraint next period plus the benefit of higher productivity next period.

8.2 Proof of Proposition 2

Proposition 2 in the text states:

Proposition 2: *In a competitive equilibrium with $\Phi(i_{j,t}) = 0$, $i_{j,t}$ is lower than optimal when $\xi < 1$.*

Proof. From Proposition 1, the social planner chooses $i_{j,t} = i_t$ and $\frac{k_{j,t}^r}{\mathcal{E}_{j,t}} = \frac{k_t^r}{\mathcal{E}_t}$. This, together with the first order condition (20), implies that

$$-\Psi'(i_t)\mathcal{E}_{j,t} \left(\frac{k_t^r}{\mathcal{E}_t}\right)^{\alpha_r} \mu_{r,t}^j = \xi\mu_{\mathcal{E},t}^j + (1-\xi)\frac{k_{j,t}^r}{k_t^r} \int_0^1 \mu_{\mathcal{E},t}^j dj. \quad (37)$$

The first order conditions of the social planner's problem also give

$$\beta^t u'(c_t) (1-\theta) A_t \frac{(k_t^c)^{\theta_k} (L_t)^{\theta_L}}{(e_t)^\theta} = \mu_{E,t} = \mu_{r,t}^j. \quad (38)$$

Equation (37) together with (38) and (30) implies

$$-\beta^t u'(c_t) p_t^e \Psi'(i_t) \mathcal{E}_{j,t} \left(\frac{k_t^r}{\mathcal{E}_t}\right)^{\alpha_r} = \xi\mu_{\mathcal{E},t}^j + (1-\xi)\frac{k_{j,t}^r}{k_t^r} \int_0^1 \mu_{\mathcal{E},t}^j dj. \quad (39)$$

The first-order condition with respect to $\mathcal{E}_{j,t+1}$ is

$$\mu_{\mathcal{E},t+1}^j \frac{1}{\mathcal{E}_{t+1}^j} + \mu_{r,t+1}^j (1-\alpha_r) \Psi(i_{j,t+1}) \left(\frac{k_{j,t+1}^r}{\mathcal{E}_{j,t+1}}\right)^{\alpha_r} = \mu_{\mathcal{E},t}^j \frac{1}{\mathcal{E}_{t+1}^j}, \quad (40)$$

which can be rewritten using condition (12) as

$$\mu_{\mathcal{E},t+1}^j + \beta^{t+1} u'(c_{t+1}) p_{t+1}^e (1-\alpha_r) e_{j,t+1}^r = \mu_{\mathcal{E},t}^j.$$

Solving for $\mu_{\mathcal{E},t}^j$, we obtain

$$\mu_{\mathcal{E},t}^j = \sum_{\tau=1}^{\infty} \beta^{t+\tau} u'(c_{t+\tau}) p_{t+\tau}^e (1-\alpha_r) e_{j,t+\tau}^r, \text{ if } \lim_{\tau \rightarrow \infty} \mu_{\mathcal{E},\tau}^j = 0. \quad (41)$$

Replacing (41) in (39) we obtain

$$\begin{aligned}
-\Psi'(i_t)\mathcal{E}_{j,t}\left(\frac{k_t^r}{\mathcal{E}_t}\right)^{\alpha_r} &= \xi \sum_{\tau=1}^{\infty} \beta^\tau \frac{u'(c_{t+\tau})p_{t+\tau}^e}{u'(c_t)p_t^e} (1-\alpha_r)e_{j,t+\tau}^r + \\
&\quad (1-\xi) \sum_{\tau=1}^{\infty} \beta^\tau \frac{u'(c_{t+\tau})p_{t+\tau}^e}{u'(c_t)p_t^e} (1-\alpha_r) \frac{k_{j,t+\tau}^r}{k_{t+\tau}^r} \int_0^1 e_{j,t+\tau}^r dj.
\end{aligned} \tag{42}$$

Solving equation (36) for $\lambda_{\mathcal{E},t}^j$, we obtain

$$\lambda_{\mathcal{E},t}^j = \sum_{\tau=1}^{\infty} \beta^{t+\tau} u'(c_{t+\tau})p_{t+\tau}^e (1-\alpha_r)e_{j,t+\tau}^r, \text{ if } \lim_{\tau \rightarrow \infty} \lambda_{\mathcal{E},\tau}^j = 0. \tag{43}$$

Finally, replacing (43) in equation (35) (with $\Phi(i_{j,t}) = 0$) gives

$$-\Psi'(i_{j,t}) (\mathcal{E}_{j,t}) \left(\frac{k_{j,t}^r}{\mathcal{E}_{j,t}}\right)^{\alpha_r} = \xi \sum_{\tau=1}^{\infty} \beta^\tau \frac{u'(c_{t+\tau})p_{t+\tau}^e}{u'(c_t)p_t^e} (1-\alpha_r)e_{j,t+\tau}^r. \tag{44}$$

It is straightforward to verify that the right hand side of equation (42) is larger than the right hand side of equation (44). Since $-\Psi'(i_{j,t})$ is increasing in $i_{j,t}$, everything else equal, the value of $i_{j,t}$ that satisfies (44) in the competitive equilibrium equation is lower than the i_t that satisfies (42) in the social planner's first order condition. ■

8.3 Proof of Proposition 3

Proposition 3 in the text states:

Proposition 3: (1) *The optimal allocation can be supported by a combination of a revenue-neutral policy, $\Phi(i_{j,t}) = -(1-\xi)p_t^e\Psi'(i_t^*)\left(\frac{e_{j,t}^{*r}}{\Psi(i_{j,t}^*)}\right)(i_{j,t} - i_t^*)$, imposed on renewable firms, together with a Pigouvian tax on fossil fuel use,*

$$\tau_t^f = \sum_{j=0}^{\infty} \beta^j \frac{u'(c_{t+j}^*)}{u'(c_t^*)} \pi_{t+j} y_{t+j}^* (1-d_j),$$

where $\{c_t^*, y_t^*, i_t^*\}_{t=0}^{\infty}$ is the solution to the planner's problem, and $1-d_j = \varphi_L + (1-\varphi_L)\varphi_0(1-\varphi)^j$. (2) *If $u(c) = \log(c)$, $\alpha_r = \alpha_f = \alpha$, $\pi_t = \pi$, all t , and $\delta = 1$, $\tau_t^f = y_t \pi \left[\frac{\varphi_L}{1-\beta} + \frac{(1-\varphi_L)\varphi_0}{1-(1-\varphi)\beta} \right]$ does not depend on the growth rate of the economy.*

Proof. When $\Phi(i_{j,t}) = -(1-\xi)p_t^e\Psi'(i_t^*)\left(\frac{e_{j,t}^{*r}}{\Psi(i_{j,t}^*)}\right)(i_{j,t} - i_t^*)$ the firm j 's first order condition (35) is

$$-\beta^t u'(c_t) \left[p_t^e \Psi'(i_t^*) \left(\frac{e_{j,t}^{*r}}{\Psi(i_{j,t}^*)} \right) \right] = \lambda_{\mathcal{E},t}^j, \tag{45}$$

Solving (36) for $\lambda_{\mathcal{E},t}^j$, we obtain

$$\lambda_{\mathcal{E},t}^j = \sum_{\tau=1}^{\infty} \beta^{t+\tau} u'(c_{t+\tau}) p_{t+\tau}^e (1 - \alpha_r) e_{j,t+\tau}^r, \text{ if } \lim_{\tau \rightarrow \infty} \lambda_{\mathcal{E},\tau}^j = 0. \quad (46)$$

Combining this equation with (45) gives

$$-\Psi'(i_t^*) (\mathcal{E}_{j,t}) \left(\frac{k_t^r}{\mathcal{E}_t} \right)^{\alpha_r} = \sum_{\tau=1}^{\infty} \beta^\tau \frac{u'(c_{t+\tau}) p_{t+\tau}^e}{u'(c_t) p_t^e} (1 - \alpha_r) e_{j,t+\tau}^r. \quad (47)$$

The social planner's problem gives rise to a similar condition, (42), which we repeat here:

$$\begin{aligned} -\Psi'(i_t) \mathcal{E}_{j,t} \left(\frac{k_t^r}{\mathcal{E}_t} \right)^{\alpha_r} &= \xi \sum_{\tau=1}^{\infty} \beta^\tau \frac{u'(c_{t+\tau}) p_{t+\tau}^e}{u'(c_t) p_t^e} (1 - \alpha_r) e_{j,t+\tau}^r + (1 - \xi) \\ &\quad \sum_{\tau=1}^{\infty} \beta^\tau \frac{u'(c_{t+\tau}) p_{t+\tau}^e}{u'(c_t) p_t^e} (1 - \alpha_r) \frac{k_{j,t+\tau}^r}{k_{t+\tau}^r} \int_0^1 e_{j,t+\tau}^r dj \end{aligned} \quad (48)$$

To show that these conditions are identical, thus implying the same i_t , it suffices to show that

$$\frac{k_{j,t}^r}{k_t^r} \int_0^1 e_{j,t}^r dj = e_{j,t}^r. \quad (49)$$

This follows from

$$\begin{aligned} \frac{k_{j,t}^r}{k_t^r} \int_0^1 e_{j,t}^r dj &= \frac{k_{j,t}^r}{\int_0^1 k_{j,t}^r dj} \int_0^1 \Psi(i_t) k_{j,t}^r \left(\frac{k_t^r}{\mathcal{E}_t} \right)^{\alpha_r - 1} dj \\ &= \frac{k_{j,t}^r}{\int_0^1 k_{j,t}^r dj} \Psi(i_t) \left(\frac{k_t^r}{\mathcal{E}_t} \right)^{\alpha_r - 1} \int_0^1 k_{j,t}^r dj \\ &= k_{j,t}^r \Psi(i_t) \left(\frac{k_t^r}{\mathcal{E}_t} \right)^{\alpha_r - 1} = e_{j,t}^r. \end{aligned} \quad (50)$$

Next, suppose that sellers of fossil fuel face a linear tax rate,

$$\tau_t^f = \sum_{j=0}^{\infty} \beta^j \frac{u'(c_{t+j}^*)}{u'(c_t^*)} \pi_{t+j} y_{t+j}^* (1 - d_j), \quad (51)$$

where $\{c_t^*, y_t^*\}_{t=0}^{\infty}$ solves the planner's problem, and $1 - d_j = \varphi_L + (1 - \varphi_L) \varphi_0 (1 - \varphi)^j$. Under this tax, the fossil-fuel-producers' optimal intertemporal substitution implies

$$u'(c_t) \cdot p_t^f = \beta u'(c_{t+1}) \cdot p_{t+1}^f. \quad (52)$$

Using (32) for the price of fossil fuel, we obtain

$$u'(c_t) \left\{ MPF_t - \tau_t^f \right\} = \beta u'(c_{t+1}) \left\{ MPF_{t+1} - \tau_{t+1}^f \right\},$$

and using (51) for the tax, we obtain

$$\begin{aligned}
& u'(c_t) \{MPF_t - \pi_t y_t^* (\varphi_L + (1 - \varphi_L)\varphi_0)\} \\
& + \sum_{j=1}^{\infty} \beta^j u'(c_{t+j}^*) \pi_{t+j} y_{t+j}^* ((1 - \varphi_L)\varphi_0 (1 - \varphi)^{j-1} \varphi) \\
& = \beta u'(c_{t+1}) \{MPF_{t+1}\},
\end{aligned} \tag{53}$$

where MPF_t is the period- t marginal productivity of fossil fuel in units of the final good. Clearly, the claim follows if $\frac{y_{t+j}^*}{c_{t+1}^*} = \chi$, a constant. First, observe that $\frac{c_t}{y_t} = \chi \Leftrightarrow \frac{k_{t+1}^g}{y_t} = \theta^k \beta$. This equation follows from the FOCs of the social planner, which include

$$\frac{y_t}{c_t} = \frac{y_{t+1}}{c_{t+1}} \frac{\theta^k \beta y_t}{k_{t+1}^g}. \tag{54}$$

It remains to be shown that

$$\frac{k_{t+1}^f}{y_t} + \frac{k_{t+1}^r}{y_t} = 1 - \chi - \theta^k \beta \equiv \varrho, \tag{55}$$

where $k_t^r = \int k_{t,m}^r dm$. The social planner problem's FOCs with respect to $k_{j,t}^r$ implies

$$\alpha_r \Psi(i_t) \left(\frac{\mathcal{E}_{j,t}}{k_{j,t}^r} \right)^{1-\alpha_r} (1-\theta) \frac{y_t}{e_t} = \alpha_r \left(\frac{e_{j,t}^r}{k_{j,t}^r} \right) (1-\theta) \frac{y_t}{e_t} = \theta^k \frac{y_t}{k_t^g} \tag{56}$$

$$\alpha_r (1-\theta) \frac{e_{j,t}^r}{e_t} = \frac{1}{\beta} \frac{k_{j,t}^r}{y_{t-1}}. \tag{57}$$

The FOC with respect to k_t^f implies

$$\alpha_f (1-\theta) \frac{e_t^f}{e_t} = \frac{1}{\beta} \frac{k_t^f}{y_{t-1}}. \tag{58}$$

It is sufficient to show that

$$\beta (1-\theta) \left(\frac{\alpha_r e_{t+1}^r + \alpha_f e_{t+1}^f}{e_{t+1}} \right) = \varrho, \tag{59}$$

which is true if $\alpha_r = \alpha_f = \alpha$. ■

8.4 The Optimal Transition

Here we characterize the equilibrium allocation across the transition, and we derive some key expressions that are used in our calibration. Let $V(k; A, L, \mathcal{E}, w; \Gamma^p, \Gamma^d)$ denote the value given k available units of capital and given that the aggregate productivity is A , the labor supply is l , the productivity in the renewable energy

sector is \mathcal{E} , the stock of fossil fuel is w , and the stocks of permanent and depreciating emissions are Γ^p and Γ^d , respectively. We let g stand for the percentage productivity growth rate in the final good sector, while g^l is the population growth rate.

The optimal consumption and saving decision under log utility and full depreciation is given by $c = (1 - \beta\Theta)y$, and $k' = \beta\Theta y$, where $\Theta = \theta_k + (1 - \theta_k - \theta_\ell)\alpha$ is the marginal product of capital. The recursive formulation for $V(\cdot)$ is given by

$$\begin{aligned}
V(k; A, L, \mathcal{E}, w; \Gamma^p, \Gamma^d) &= \max_{i, f} \{ \ln((1 - \beta\Theta)y) \\
&\quad + \beta V(\beta\Theta y; gA, g^l, e^i \mathcal{E}, w - f; \Gamma^{p'}, \Gamma^{d'}) \} \\
&\text{where} \\
y &= e^{-\pi(\Gamma^{p'} + \Gamma^{d'} - \bar{\Gamma})} AL^{\theta_\ell} \left(f + \Psi(i)^{\frac{1}{1-\alpha}} \mathcal{E} \right)^{(1-\alpha)(1-\theta_k-\theta_\ell)} k^\Theta \\
\Gamma^{p'} &= \Gamma^p + \varphi_L f \\
\Gamma^{d'} &= (1 - \varphi)\Gamma^d + (1 - \varphi_L)\varphi_0 f.
\end{aligned} \tag{60}$$

Utilizing the envelope theorem, we have $V_k = \Theta \frac{1}{k} + \beta\Theta \frac{k'}{k} V_{k'}$, which implies

$$kV_k = \Theta + \beta\Theta k' V_{k'}. \tag{61}$$

We guess that kV_k is a constant and we verify that

$$V_k = \frac{\Theta}{1 - \beta\Theta} \frac{1}{k}. \tag{62}$$

Using the same method, we have that $V_A = \frac{1}{A} + \beta \left\{ \frac{k'}{A} V_{k'} + gV_{A'} \right\}$, which, in turn, implies

$$AV_A = 1 + \beta \left\{ \frac{\Theta}{1 - \beta\Theta} + (gA) V_{A'} \right\}. \tag{63}$$

Next, we guess that AV_A is a constant. As $A' = gA$, this equation allows us to verify that

$$V_A = \frac{1}{(1 - \beta)(1 - \beta\Theta)} \frac{1}{A}. \tag{64}$$

Similarly, we obtain

$$V_L = \frac{\theta_l}{(1 - \beta)(1 - \beta\Theta)} \frac{1}{L}, \tag{65}$$

$$V_{\Gamma^p} = \frac{1}{(1 - \beta)(1 - \beta\Theta)} (-\pi), \tag{66}$$

$$V_{\Gamma^d} = \frac{1 - \varphi}{(1 - \beta(1 - \varphi))(1 - \beta\Theta)} (-\pi). \tag{67}$$

The last expression reflects the depreciation rate of the temporary part of the emissions stock. Finally, the marginal value of stock of fossil fuel is given by

$$V_w = \beta \cdot V'_{w-f}.$$

The optimal choice of f on the equilibrium path implies

$$\frac{(1-\alpha)(1-\theta_k-\theta_\ell)}{f+\Psi(i)^{\frac{1}{1-\alpha}}\mathcal{E}}(1+\beta\cdot k'V'_{k'})\leq V_w+\tau\left\{\begin{array}{l}\pi\cdot(\varphi_L+(1-\varphi_L)\varphi_0)(1+\beta\cdot k'V'_{k'}) \\ -\beta[\varphi_L V'_{\Gamma^{p'}}+(1-\varphi_L)\varphi_0 V'_{\Gamma^{d'}}]\end{array}\right\},$$

with equality when $f > 0$. The left-hand side of the above inequality gives the marginal benefit from consumption and from future capital accumulation, respectively. The first term of the right-hand side, $V_w = \beta V'_{w-f}$, is the price of fossil fuel. The second term is the tax on consumption of fossil fuel. Note that $\tau \in [0, 1]$, so this tax could take any value from zero to the total value of the present and future damages resulting from GHG emissions. We will find it convenient to rewrite the above inequality as follows:

$$f+\Psi(i)^{\frac{1}{1-\alpha}}\mathcal{E}\geq\frac{(1-\alpha)(1-\theta_k-\theta_\ell)}{\tau\pi\left\{\frac{\varphi_L}{1-\beta}+\frac{(1-\varphi_L)\varphi_0}{1-\beta(1-\varphi)}\right\}+(1-\beta\Theta)V_w},\quad(68)$$

with equality for $f > 0$. For $f, f' > 0$, using $V_w = \beta V'_w$, and (85) we obtain:

$$\left(f+\Psi(i)^{\frac{1}{1-\alpha}}\mathcal{E}\right)^{-1}=\beta\left(f'+\Psi(i')^{\frac{1}{1-\alpha}}\mathcal{E}'\right)^{-1}+(1-\beta)\frac{\tau\pi\left\{\frac{\varphi_L}{1-\beta}+\frac{(1-\varphi_L)\varphi_0}{1-\beta(1-\varphi)}\right\}}{(1-\alpha)(1-\theta_k-\theta_\ell)}.\quad(69)$$

We use equation (86) to find the equilibrium path of fossil fuel consumption by solving this path backward. To do so, we also need to determine the equilibrium path of the renewable energy productivity.

The optimal choice for i , when the representative agent takes into account only ξ fraction of the benefit of higher i on future renewable productivity, implies

$$0=(1-\alpha)(1-\theta_k-\theta_\ell)\frac{\frac{1}{1-\alpha}\Psi'(i)\Psi(i)^{\frac{1}{1-\alpha}-1}\mathcal{E}}{f+\Psi(i)^{\frac{1}{1-\alpha}}\mathcal{E}}\left\{1+\beta\frac{\Theta}{1-\beta\Theta}\right\}+\beta\cdot\xi\underbrace{e^i\mathcal{E}}_{\mathcal{E}'}V'_{\mathcal{E}'},\quad(70)$$

or

$$\frac{-\Psi'(i)}{\Psi(i)}\frac{(1-\theta_k-\theta_\ell)}{1-\beta\Theta}\frac{\Psi(i)^{\frac{1}{1-\alpha}}\mathcal{E}}{f+\Psi(i)^{\frac{1}{1-\alpha}}\mathcal{E}}=\beta\cdot\xi\mathcal{E}'V'_{\mathcal{E}'}. \quad(71)$$

Utilizing the envelope theorem, we have

$$\mathcal{E}V_{\mathcal{E}}=\frac{(1-\alpha)(1-\theta_k-\theta_\ell)}{1-\beta\Theta}\frac{\Psi(i)^{\frac{1}{1-\alpha}}\mathcal{E}}{f+\Psi(i)^{\frac{1}{1-\alpha}}\mathcal{E}}+\beta\mathcal{E}'V'_{\mathcal{E}'}. \quad(72)$$

Combining the above equation with (71), we obtain

$$\frac{-\Psi'(i)}{\Psi(i)}=\beta\cdot\frac{\frac{\Psi(i')^{\frac{1}{1-\alpha}}\mathcal{E}'}{f'+\Psi(i')^{\frac{1}{1-\alpha}}\mathcal{E}'}}{\frac{\Psi(i)^{\frac{1}{1-\alpha}}\mathcal{E}}{f+\Psi(i)^{\frac{1}{1-\alpha}}\mathcal{E}}}\left(\xi(1-\alpha)+\frac{-\Psi'(i')}{\Psi(i')}\right).\quad(73)$$

Equation (87) shows how the evolution of the elasticity of the technology adoption cost with respect to the adoption rate, $\frac{-\Psi'}{\Psi}$, between two consecutive periods depends on the corresponding ratio of the share of renewable energy, $\frac{\Psi(i)^{\frac{1}{1-\alpha}} \mathcal{E}}{f + \Psi(i)^{\frac{1}{1-\alpha}} \mathcal{E}}$. To determine the path of i and f , we begin by determining \hat{i} , the long-run i . On a long-run balanced growth path, we have $f = f' = 0$, and $i = i' = \hat{i}$, where \hat{i} is determined by

$$\frac{-\Psi'(\hat{i})}{\Psi(\hat{i})} = \frac{\beta}{1-\beta} \cdot \xi(1-\alpha). \quad (74)$$

The minimum \mathcal{E} for which f is zero follows from (85):

$$\Psi(\hat{i})^{\frac{1}{1-\alpha}} \underline{\mathcal{E}} = \frac{(1-\alpha)(1-\theta_k - \theta_\ell)}{\tau\pi \left\{ \frac{\varphi_L}{1-\beta} + \frac{(1-\varphi_L)\varphi_0}{1-\beta(1-\varphi)} \right\}}. \quad (75)$$

Note that $\underline{\mathcal{E}} < \infty$ only if $\tau > 0$. The representative agent could exhaust the stock of fossil fuel before the productivity of the renewable energy reaches $\underline{\mathcal{E}}$, in which case the price of fossil fuel will be positive. However, once $\mathcal{E} \geq \underline{\mathcal{E}}$, the stock of fossil fuel is not exhausted.

In the period right before the use of fossil fuel ends; i.e., when $f > f' = 0$, following (87) and given that $i' = \hat{i}$, we have:

$$\begin{aligned} \frac{-\Psi'(i)}{\Psi(i)} &= \beta \cdot \frac{f + \Psi(i)^{\frac{1}{1-\alpha}} \mathcal{E}}{\Psi(i)^{\frac{1}{1-\alpha}} \mathcal{E}} \left(\xi(1-\alpha) + \frac{-\Psi'(\hat{i})}{\Psi(\hat{i})} \right) \\ &= \beta \cdot \frac{f + \Psi(i)^{\frac{1}{1-\alpha}} \mathcal{E}}{\Psi(i)^{\frac{1}{1-\alpha}} \mathcal{E}} \cdot \frac{\xi(1-\alpha)}{1-\beta}. \end{aligned} \quad (76)$$

Substituting $f' = 0$ in (86) to solve for $f + \Psi(i)^{\frac{1}{1-\alpha}} \mathcal{E}$, and noting that $\mathcal{E} = e^{-i} \mathcal{E}'$, the above equation gives:

$$\frac{-\Psi'(i)}{\Psi(i)} \cdot \underbrace{\Psi(i)^{\frac{1}{1-\alpha}} e^{-i} \mathcal{E}'}_{\mathcal{E}} = \beta \cdot \frac{1}{\frac{\beta}{\Psi(i)^{\frac{1}{1-\alpha}} \mathcal{E}'} + \frac{(1-\beta)}{\tau\pi \left\{ \frac{\varphi_L}{1-\beta} + \frac{(1-\varphi_L)\varphi_0}{1-\beta(1-\varphi)} \right\}}} \cdot \frac{\xi(1-\alpha)}{1-\beta}, \quad (77)$$

which uniquely determines i , given the next period's productivity, \mathcal{E}' . Given i and utilizing (86), we have:

$$\tilde{f} = \frac{1}{\frac{\beta}{\Psi(i)^{\frac{1}{1-\alpha}} \mathcal{E}'} + \frac{(1-\beta)}{\tau\pi \left\{ \frac{\varphi_L}{1-\beta} + \frac{(1-\varphi_L)\varphi_0}{1-\beta(1-\varphi)} \right\}}} - \underbrace{\Psi(i)^{\frac{1}{1-\alpha}} e^{-i} \mathcal{E}'}_{\mathcal{E}}. \quad (78)$$

Note that \tilde{f} is the maximum level of fossil fuel consumption prior to ending its use. That is, if the stock of remaining fossil fuel was larger than \tilde{f} , some

of the fossil fuel would be left for consumption in the next period.¹⁸ Thus, it is possible that the stock of remaining fossil fuel is in fact lower than \tilde{f} . In such cases, equation (86) does not hold, since $f' = 0$ and (85) is an inequality. Nevertheless, for any value of $f < \tilde{f}$ we can determine i simply by noting that $\mathcal{E} = e^{-i}\mathcal{E}'$ and using:

$$\frac{-\Psi'(i)}{\Psi(i)} \cdot \frac{\Psi(i)^{\frac{1}{1-\alpha}} e^{-i}\mathcal{E}'}{f + \Psi(i)^{\frac{1}{1-\alpha}} e^{-i}\mathcal{E}'} = \beta \cdot \frac{\xi(1-\alpha)}{1-\beta}. \quad (79)$$

When $f, f' > 0$, using (86) to solve for $f + \Psi(i)^{\frac{1}{1-\alpha}}\mathcal{E}$ in (87) and noting that $\mathcal{E} = e^{-i}\mathcal{E}'$ we obtain:

$$\begin{aligned} \frac{-\Psi'(i)}{\Psi(i)} \underbrace{\Psi(i)^{\frac{1}{1-\alpha}} e^{-i}\mathcal{E}'}_{\mathcal{E}} &= \beta \cdot \frac{1}{\frac{\beta}{f + \Psi(i')^{\frac{1}{1-\alpha}}\mathcal{E}'} + \frac{(1-\beta)}{\frac{(1-\alpha)(1-\theta_k-\theta_\ell)}{\tau\pi\left\{\frac{\varphi L}{1-\beta} + \frac{(1-\varphi)L\varphi_0}{1-\beta(1-\varphi)}\right\}}}} \cdot \frac{\Psi(i')^{\frac{1}{1-\alpha}}\mathcal{E}'}{f' + \Psi(i')^{\frac{1}{1-\alpha}}\mathcal{E}'} \\ &\times \left(\xi(1-\alpha) + \frac{-\Psi'(i')}{\Psi(i')} \right), \end{aligned} \quad (80)$$

which allows us to uniquely determine i for a given \mathcal{E}' , i' , and f' . Then, using i and (86), we obtain the equilibrium path f :

$$f = \frac{1}{\frac{\beta}{f' + \Psi(i')^{\frac{1}{1-\alpha}}\mathcal{E}'} + \frac{(1-\beta)}{\frac{(1-\alpha)(1-\theta_k-\theta_\ell)}{\tau\pi\left\{\frac{\varphi L}{1-\beta} + \frac{(1-\varphi)L\varphi_0}{1-\beta(1-\varphi)}\right\}}}} - \underbrace{\Psi(i)^{\frac{1}{1-\alpha}} e^{-i}\mathcal{E}'}_{\mathcal{E}}. \quad (81)$$

By using this backward calculation we can determine the entire equilibrium path for all possible initial stock of fossil fuel and renewable productivity levels.¹⁹

Finally, if $f = 0$, we have:

$$V_{\mathcal{E}} = \frac{(1-\alpha)(1-\theta_k-\theta_\ell)}{(1-\beta)(1-\beta\Theta)} \frac{1}{\mathcal{E}}. \quad (82)$$

Hence,

$$\begin{aligned} V(k; A, L, \mathcal{E}; 0, \Gamma^p, \Gamma^d) &= C + \frac{\Theta}{1-\beta\Theta} \ln k \\ &+ \frac{1}{(1-\beta)(1-\beta\Theta)} \{ \ln A + \theta_l \ln L + (1-\alpha)(1-\theta_k-\theta_\ell) \ln \mathcal{E} \} \\ &- \frac{\pi}{(1-\beta)(1-\beta\Theta)} \Gamma^p - \frac{\pi(1-\varphi)}{(1-(1-\varphi)\beta)(1-\beta\Theta)} \Gamma^d, \end{aligned} \quad (83)$$

¹⁸Equation (86) holds when both f and f' are positive, but it also holds if $f = \tilde{f}$ and (85) holds with equality for $f' = 0$.

¹⁹We can show that going backward, i converges to \hat{i}^f determined by

$$\frac{-\Psi'(\hat{i}^f)}{\Psi(\hat{i}^f)} = \frac{\beta e^{\hat{i}^f}}{1 - \beta e^{\hat{i}^f}} (1-\alpha),$$

where $\hat{i}^f > \hat{i}$.

where C is a constant. Note that log utility, full depreciation, and the structure of the damage function imply that the above expression is linear in Γ^p and Γ^d .

8.5 Productivity Growth in the Fossil Fuel Sector

Here we characterize the equilibrium allocation across the transition in an extension of the model where we allow for growth in fossil fuel sector. We let $V(k; A, A_f, L, \mathcal{E}, w; \Gamma^p, \Gamma^d)$ denote the value given that the productivity of the fossil fuel sector is A_f and the growth in productivity of the fossil fuel sector is g^f .

The recursive formulation for $V(\cdot)$ is given by

$$\begin{aligned}
V(k; A, A_f, L, \mathcal{E}, w; \Gamma^p, \Gamma^d) &= \max_{i, f} \{ \ln((1 - \beta\Theta)y) \\
&\quad + \beta V(\beta\Theta y; gA, g^f A_f, g^l l, e^i \mathcal{E}, w - f; \Gamma^{p'}, \Gamma^{d'}) \} \\
&\text{where} \\
y &= e^{-\pi(\Gamma^{p'} + \Gamma^{d'} - \bar{\Gamma})} AL^{\theta_\ell} \left(A_f f + \Psi(i)^{\frac{1}{1-\alpha}} \mathcal{E} \right)^{(1-\alpha)(1-\theta_k-\theta_\ell)} k^\Theta, \\
\Gamma^{p'} &= \Gamma^p + \varphi_L f, \\
\Gamma^{d'} &= (1 - \varphi)\Gamma^d + (1 - \varphi_L)\varphi_0 f.
\end{aligned} \tag{84}$$

Proceeding as before, we obtain:

$$f + \Psi(i)^{\frac{1}{1-\alpha}} \frac{\mathcal{E}}{A_f} \geq \frac{(1 - \alpha)(1 - \theta_k - \theta_\ell)}{\tau\pi \left\{ \frac{\varphi_L}{1-\beta} + \frac{(1-\varphi_L)\varphi_0}{1-\beta(1-\varphi)} \right\} + (1 - \beta\Theta)V_w}, \tag{85}$$

with equality for $f > 0$. For $f, f' > 0$, using $V_w = \beta V'_w$, and (85) we obtain:

$$\frac{1}{f + \Psi(i)^{\frac{1}{1-\alpha}} \frac{\mathcal{E}}{A_f}} = \frac{\beta}{f' + \Psi(i')^{\frac{1}{1-\alpha}} \frac{\mathcal{E}'}{A'_f}} + \frac{1 - \beta}{\tau\pi \left\{ \frac{\varphi_L}{1-\beta} + \frac{(1-\varphi_L)\varphi_0}{1-\beta(1-\varphi)} \right\}}. \tag{86}$$

Like before, we use equation (86) to find the equilibrium path of fossil fuel consumption by solving this path backward. The equation determining the optimal choice for i together with the envelope theorem implies:

$$\frac{-\Psi'(i)}{\Psi(i)} = \beta \cdot \frac{\frac{\Psi(i')^{\frac{1}{1-\alpha}} \mathcal{E}'}{A'_f f' + \Psi(i')^{\frac{1}{1-\alpha}} \mathcal{E}'}}{\frac{\Psi(i)^{\frac{1}{1-\alpha}} \mathcal{E}}{A_f f + \Psi(i)^{\frac{1}{1-\alpha}} \mathcal{E}}} \left(\xi(1 - \alpha) + \frac{-\Psi'(i')}{\Psi(i')} \right). \tag{87}$$

Equation (87) shows how the evolution of the elasticity of the technology adoption cost with respect to the adoption rate, $\frac{-\Psi'}{\Psi}$, in two consecutive periods depends on the corresponding ratio of the share of renewable energy, $\frac{\Psi(i)^{\frac{1}{1-\alpha}} \mathcal{E}}{A_f f + \Psi(i)^{\frac{1}{1-\alpha}} \mathcal{E}}$.

The minimum \mathcal{E} for which f is zero follows from (85):

$$\Psi(\hat{i})^{\frac{1}{1-\alpha}} \frac{\mathcal{E}}{A_f} = \frac{(1-\alpha)(1-\theta_k-\theta_\ell)}{\tau\pi \left\{ \frac{\varphi_L}{1-\beta} + \frac{(1-\varphi_L)\varphi_0}{1-\beta(1-\varphi)} \right\}}. \quad (88)$$

8.6 Calibrating the Spillover Externality

Here we discuss an alternative way of calibrating ξ , the parameter capturing the importance of spillovers in innovation in the renewable energy sector. Although coming from a different viewpoint, this method results in a similar value to the one we use in the paper. In our model, the spillover externality depends on the aggregate amounts of investment and capital stock in the renewable energy sector and affects the firms' productivity. While measuring the direct effect of spillovers on productivity is challenging, one approach is to concentrate on knowledge spillovers. If knowledge, innovation, and productivity improvements are proportional to each other, then quantifying knowledge spillovers can be informative about the magnitude of spillovers in actual productivity improvements. It is common to use patents as a measure of acquired knowledge, and patent citations as a measure of the reliance of new discoveries on existing knowledge. Cross-citations can then serve as a measure of connectivity across different technologies, sectors, or geographic locations.

To get a handle on knowledge spillovers related to renewable energy, we investigate the interconnections between new and existing patents in renewable technologies. While we did not have access to cross citations across individual firms, Conti et al (2018) document aggregate cross-citations in renewable technology between the US, the EU, and Japan during the period 2000-2010. These are summarized below:

Citing country	Domestic	Foreign
EU	.76	.24
Japan	.61	.39
US	.42	.58

For example, assuming ergodicity, this would imply that the average new EU patent citations constitute 76 percent of existing EU patents and 24 percent of existing Japanese and US patents, etc. Simple averaging would lead to a ξ of .59, which is quite close to the calibrated value of 0.54 used in the paper.

8.7 Lack of Commitment

In order to explore the implications of commitment, here we briefly consider an extension of the model in the main text. Suppose that the government experiences “electoral death” with probability ω in each period. More precisely, for any period t , with probability $\omega \in (0, 1]$, the government learns at the end of t , that it will not be around at the beginning of period $t + 2$. The implied discounting sequences for the government, β^G , and for the representative agent, β^A , respectively, are given by:

$$\begin{aligned}
\beta^G &= \{1, \beta, \beta^2(1-\omega), \beta^3(1-\omega)^2, \dots\} \\
\beta^A &= \{1, \beta, \beta^2, \beta^3, \dots\}
\end{aligned} \tag{89}$$

We assume lack of commitment.²⁰ Thus, at the beginning of each period, the taxes and subsidies are set for the current period. We examine the case where $\xi = 1$, so there are no technology spillovers and the only externality is the one associated with GHG emissions. In each period, the government chooses the Pigouvian tax rate on fossil fuel consumption, τ_t^f . Under no commitment, this tax needs to be set in a time-consistent fashion. The optimal allocation can again be supported by a Pigouvian tax on emissions. This tax is lower than the case studied in the earlier model.

The government's objective is a modified version of the planner's objective in the previous section and it is given by:

$$u(c_0) + \sum_{t=1}^{\infty} (1-\omega)^{t-1} \beta^t u(c_t) \tag{90}$$

All feasibility constraints remain the same. As a result, the optimal allocation is characterized by similar FOCs as in the previous section, with the only modification being in the discount sequence. We can demonstrate the following.

Proposition 4 (1) *The government's optimal allocation can be supported by a Pigouvian tax given by $\tau_t^f = \pi_t y_t^* (1-d_0) + \sum_{j=1}^{\infty} (1-\omega)^{j-1} \beta^j \frac{u'(c_{t+j}^*)}{u'(c_t^*)} \pi_{t+j} y_{t+j}^* (1-d_j)$, where $\{c_t^*, y_t^*, i_t^*\}_{t=0}^{\infty}$ is the solution to the government's problem, and $1-d_j = \varphi_L + (1-\varphi_L)\varphi_0(1-\varphi)^j$. (2) If $u(c) = \log(c)$, $\alpha_r = \alpha_f = \alpha$, $\pi_t = \pi$, all t , and $\delta = 1$, then $\tau_t^f = y_t \pi \left[\varphi_L + (1-\varphi_L)\varphi_0 + \frac{\beta\varphi_L}{1-(1-\omega)\beta} + \frac{\beta(1-\varphi)(1-\varphi_L)\varphi_0}{1-(1-\omega)(1-\varphi)\beta} \right]$ does not depend on the growth rate of the economy. (3) *The tax is strictly lower than the optimal Pigouvian tax of the previous section for all t .**

8.8 A Continuous Time Interpretation

Here we provide a continuous-time foundation of our modeling of the scrapping process in the main text. The instantaneous production function in this case is given by:

$$e_j^r(t) = [\mathcal{E}_j(t)]^{1-\alpha_r} [k_j^r(t)]^{\alpha_r}. \tag{91}$$

As the new technology adoption rate, $i_j(t)$, requires scrapping of current capital, capital evolves according to:

$$\frac{dk_j^r(t)}{k_j^r(t)} = -f(i_j(t))dt, \tag{92}$$

²⁰See Harstad (2019) for a discussion of time inconsistency in a related model.

where $f' > 0$. Adoption of a newer technology, $i_j(t)$, improves the productivity of firm j according to

$$\frac{d\mathcal{E}_j(t)}{\mathcal{E}_j(t)} = g(i_j(t))dt, \quad (93)$$

where $g' > 0$. The resulting change in production is

$$de_j^r(t) = \alpha_r [\mathcal{E}_j(t)]^{1-\alpha_r} [k_j^r(t)]^{\alpha_r-1} dk_j^r(t) + (1 - \alpha_r) [\mathcal{E}_j(t)]^{-\alpha_r} [k_j^r(t)]^{\alpha_r} d\mathcal{E}_j(t). \quad (94)$$

After replacing for the $\mathcal{E}_j(t)$ and $k_j^r(t)$ processes, we obtain

$$de_j^r(t) = \Psi[i_j(t)] [\mathcal{E}_j(t)]^{1-\alpha_r} [k_j^r(t)]^{\alpha_r} dt. \quad (95)$$

where $\Psi[i_j(t)] \equiv (1 - \alpha_r)g(i_j(t)) - \alpha_r f(i_j(t))$. We assume that $\Psi' < 0$.

References

- [1] Acemoglu, D., P. Aghion, L. Bursztyn, and D. Hemous (2012): “The Environment and Directed Technical Change,” *American Economic Review* 102(1) p. 131-166
- [2] Acemoglu, D., U. Akcigit, D. Hanley, and W. Kerr (2016): “Transition to Clean Technology,” *Journal of Political Economy*, vol. 124, no. 1
- [3] Arrow, K.J. (1962): “Economic Welfare and the Allocation of Resources for Invention,” in R. Nelson, ed., *The Rate and Direction of Inventive Activity*. Princeton University Press
- [4] Arrow, K.J. (1962): “The economic Implications of Learning by Doing,” *Review of Economic Studies* 29
- [5] Atkeson A., and A. Burstein (2015): “Aggregate Implications of Innovation Policy,” UCLA Manuscript
- [6] Benhabib J., and A. Rustichini (1991): “Vintage capital, investment, and growth,” *Journal of Economic Theory* 55(2), p. 323-339
- [7] Bentham, A., K. Gillingham, and J. Sweeney (2008): “Learning-by-Doing and the Optimal Solar Policy in California,” *The Energy Journal* 29(3) p. 131–152

- [8] Bosettia, V., Carraro, C., Massettia, E. and M. Tavon (2008): “International energy R&D spillovers and the economics of greenhouse gas atmospheric stabilization,” *Energy Economics* 30(6), p. 2912–2929
- [9] Boucekkine, R., De La Croix, D., and O. Licandro (2017): “Vintage Capital,” in *The New Palgrave Dictionary of Economics*, Durlauf S.N., Blume L.E. (eds), Palgrave Macmillan, p. 2912–2929
- [10] Braun, F., Schmidt-Ehmcke, J., and P. Zloczysti (2009): “Innovative Activity in Renewable Energy Technologies: Empirical Evidence on Knowledge Spillovers Using Patent Data,” Manuscript
- [11] Cason, T.N., and C.R. Plott (1994): “EPA’s New Emissions Trading Mechanism: A Laboratory Evaluation,” *Journal of Environmental Economics and Management* 30
- [12] Chari, V.V., and Hugo A. Hopenhayn (1991): “Vintage Human Capital, Growth and the Diffusion of New Technologies,” *Journal of Political Economy*
- [13] Chakravorty, U., Roumasset J., and K. Tse (1997): “Endogenous Substitution among Energy Resources and Global Warming,” *Journal of Political Economy* 105(6)
- [14] Conti, C., M.L. Mancusi, F. Sanna-Randaccio, R. Sestini, E. Verdolini (2018): “Transition towards a green economy in Europe: Innovation and knowledge integration in the renewable energy sector,” *Research Policy* 47(10), pp. 1996-2009
- [15] Fried, Stephanie (2018): “Climate Policy and Innovation: A Quantitative Macroeconomic Analysis,” *American Economic Journal: Macroeconomics* 10 (1): 90-118

- [16] Gautam Gowrisankaran, G., and M. Rysman (2012): “Dynamics of Consumer Demand for New Durable Goods,” *Journal of Political Economy* 120(6) , pp. 1173-1219
- [17] Goulder, Lawrence H., and Stephen H. Schneider (1999): “Induced Technological Change and the Attractiveness of CO₂ Abatement Policies,” *Resource and Energy Economics* 21(3–4), p. 211–53
- [18] Golosov M., J. Hassler, P. Krusell, and A. Tsyvinski (2014): “Optimal Taxes on Fossil Fuel in General Equilibrium,” *Econometrica*, 82(1), p. 41-88
- [19] Graubler, A., and S. Messner (1998): “Technological Change and the Timing of Mitigation Measures”, *Energy Economics* 20, p. 495–512
- [20] Greenwood J., Hercowitz Z., and P. Krusell (1997): “Long-Run Implications of Investment-Specific Technological Change,” *American Economic Review* 87(3), p. 342-362
- [21] Harstad, B. (2019): “Technology and Time Inconsistency” *Journal of Political Economy*, forthcoming
- [22] Hartley, P., and K. Medlock III (2005): “Carbon Dioxide: A Limit to Growth?” Manuscript
- [23] Hartley P., Medlock III K., Temzelides T., and X. Zhang (2016): “Energy Sector Innovation and Growth,” *The Energy Journal* 37(1)
- [24] Hassler J., P. Krusell, and C. Olovsson (2011): “Energy Saving Technical Change,” mimeo, Institute of International Economic Studies, Stockholm University
- [25] Hassler J., P. Krusell, C. Olovsson, and M. Reiter (2020): “On the Effectiveness of Climate Policies,” Working paper, IIES Stockholms universitet

- [26] Hopenhayn, H. (1992): “Entry, Exit, and Firm Dynamics in Long Run Equilibrium,” *Econometrica* 60, No. 5
- [27] IPCC (2012): *Renewable Energy Sources and Climate Change Mitigation*, Special Report of the Intergovernmental Panel on Climate Change, Technical Support Unit Working Group III, Potsdam Institute for Climate Impact Research (PIK)
- [28] Jovanovic, B., and Y. Yatsenko (2012): “Investment in vintage capital,” *Journal of Economic Theory* 147(2), p. 551-569
- [29] Jovanovic, B., and S. Lach (1989): “Entry, Exit, and Diffusion with Learning by Doing,” *American Economic Review* 79, No. 4
- [30] Klaassen, G., A. Miketa, K. Larsen, and T. Sundqvist (2005): “The Impact of R&D on Innovation for Wind Energy in Denmark, Germany and the United Kingdom,” *Ecological Economics*, 54
- [31] Klette, T.J., and S. Kortum (2004): “Innovating Firms and Aggregate Innovation,” *Journal of Political Economy* 112 (5)
- [32] Lucas, R.E., Jr. (1987): “Models of Business Cycles,” *Oxford: Blackwell*, ISBN 978-0631147893
- [33] Li, X., Narajabad B., and T. Temzelides (2016): “Robust Dynamic Energy Use and Climate Change,” *Quantitative Economics* 7, p. 821-857
- Lucas, Robert E., Jr. (1987). *Models of Business Cycles*. Oxford: Blackwell. ISBN 978-0631147893
- [34] Manuelli, R., and A. Seshadri (2014): “Frictionless Technology Diffusion: The Case of Tractors,” *American Economic Review* 104(4), p. 1368-91
- [35] Mauritzen J. (2012): “Scraping a Wind Turbine: Policy Changes, Scraping Incentives and Why Wind Turbines in Good Locations Get Scrapped

First,” IFN Working Paper No. 940, Research Institute of Industrial Economics, Stockholm, Sweden

- [36] Nordhaus, William D. (1994): *Managing the Global Commons: The Economics of Climate Change*. Cambridge, MA: MIT Press
- [37] Nordhaus, William, and Joseph Boyer (2000): *Warming the World: Economic Modeling of Global Warming*. Cambridge, MA: MIT Press
- [38] Parente, Stephen L. (1994): “Technology Adoption, Learning-by-Doing and Economic Growth,” *Journal of Economic Theory*, 63(2), p. 346–369
- [39] Popp, David (2004): “ENTICE: Endogenous Technological Change in the DICE Model of Global Warming,” *Journal of Environmental Economics and Management* 48(1), p. 742–68
- [40] Solow, R.M., and F.Y. Wan (1976): “Extraction Costs in the Theory of Exhaustible Resources,” *Bell Journal of Economics*, The RAND Corporation, vol. 7(2), p. 359-370
- [41] Stern, N. (2007): *The Economics of Climate Change: The Stern Review*, Cambridge University Press
- [42] Stokey, Nancy L. (1998): “Are There Limits to Growth?” *International Economic Review* 39(1), p. 1–31
- [43] Van der Ploeg, F., and C. Withagen (2011): “Is There Really a Green Paradox?” *OxCarre Research Paper* 35
- [44] Van der Ploeg, F., and A. Rezai (2016): “Stranded Assets, the Social Cost of Carbon, and Directed Technical Change: Macroeconomic Dynamics of Optimal Climate Policy,” *CESifo Working paper* no. 5787
- [45] van der Zwaan, B. C., R. Gerlagh, G. Klaassen, and L. Schrattenholzer (2002): “Endogenous Technological Change in Climate Change Modelling,” *Energy Economics* 24(1), p. 1–19