Reminders:
1. Next homework is due Wednesday after break
2. Next exam is a take-home; handed out 3/17/00, due 3/20/00 (5pm).

Review
1. We introduced a new Scheme construct, local, that creates a new name space. We worked an example, and talked about how local works.

Local
Local takes two complicated arguments

\[(\text{local} \ [ \text{<defines>} \ ] \ <\text{expression}>)]\]

where <defines> is a set of one or more definitions, and <expression> is a Scheme expression that will be evaluated. Local creates a new name space, or context, or scope. It evaluates the definitions in that new context (which creates all the objects that they specify), and then it evaluates the expression inside that context. Once the expression has been evaluated, its value becomes the value of the local, replacing the entire local construct (and destroying its context)

Notice that the syntax is

\[(\text{local} \ ( \text{(defines)} \ ) \ (\text{expression}) \ )\]

The first argument to local is a list of definitions. The list is enclosed in parentheses. Here's another example.

\[
\text{(define (exp-5 x)}
\text{\quad (local ((define (square y) (* y y))}
\text{\quad\quad (define (cube z) (* z (square z)))})
\text{\quad (* (square x) (cube x))})
\]

If we type this into the definitions window, click execute, and go to the interactions window and evaluate (exp-5 2), DrScheme complains bitterly. We need to move to the Intermediate language level.

Once we've done that, we can evaluate (+ (exp-5 2) 3)
To evaluate the local, DrScheme copies the definitions of square and cube to the definitions window, executes them, and then evaluates

\((\text{square} \ 2) \ (\text{cube} \ 2)\)

by creating

\(\ (\ast \ (* \ 2 \ 2) \ (* \ 2 \ (\text{square} \ 2))\)\)

\(\Rightarrow \ (* \ 4 \ (* \ 2 \ (* \ 2 \ 2))\)\)

\(\Rightarrow \ (* \ 4 \ (* \ 2 \ 4))\)

\(\Rightarrow \ (* \ 4 \ 8)\)

\(\Rightarrow \ 32\)

Now comes the tricky part. Remember, the local was executing in the context of

\(\Rightarrow \ (+ \ (<\text{huge local mess}> \ 3))\)

DrScheme replaces <huge local mess> with 32. As if by magic, it then loses the ability to reference these recently created definitions of square and cube. This creates the expression

\(\Rightarrow \ (+ \ 32 \ 3)\)

\(\Rightarrow \ 35\)

What happens if we hand evaluate (cube 2)? **DrScheme gives us an error.** Why? Because **cube** exists only inside the new name space created by the local.

**Digression:** How does DrScheme really implement local? The simplest model for DrScheme's behavior is that DrScheme systematically renames all of the names created inside a **local**. For each name defined inside the local, DrScheme creates a unique new name. Next, it rewrites the expression part of the local to replace the original names with these new, unique names. Finally, it enters the definitions part of the local into the interactions window (to install them in the environment where the local's expression-part will execute), then evaluates the expression.

Even with nested locals, this resolves all of the naming conflicts. With nested locals, it performs the rewriting as the locals are encountered. The inner local is inside the expression portion of the outer local, so it gets rewritten to reflect the names installed by the outer local. Then, when the inner local begins to evaluate, it gets rewritten again with new names. Work an example by hand; it all works in a rather pretty way.
But this seems counter-intuitive…

Local gives us a glimpse under the covers of how the Scheme implementation really works. Every time you define a name, you really specify where that name may be used. For example, when you type a name at DrScheme in the interactions window, it responds with an **error** unless there has been a corresponding **define** for that name in the definitions window.

```
> x
reference to undefined identifier: x
```

But if we type

```
(define (f x) (+ x 3))
```

in the definitions window, DrScheme is perfectly happy with our use of x. Why? Because the header for the function f implicitly creates the name x—with an implicit understanding that the name x only exists inside the parentheses that bound the definition of f. These argument names (or parameter names) that we have been using all semester are actually names with a limited scope—a limited region in the code where they can be used. This idea isn't new to us; in fact, it should be familiar to us.

Local creates such a scope. The parentheses that enclose the local construct are the bounds of the scope. One difference between a local "scope" and a function "scope" is that we can use "define" inside a local (and not inside a function). Of course, that means that we can use anything that can legally appear inside a define within a local—including a local. This creates the possibility for nesting locals.

```
(define (fee a)
  (local [(define x 2)]
    (local [(define y 3)] (* a x y))))
```

and so on… The evaluation rules make it clear what happens. What about

```
(define (fie a)
  (local [(define x 2)]
    (local
      [(define y 3)]
      (local [(define x 17)]
        (* a x y)))))
```

What's the value of (fie 1)? => 51

The definition of x in the innermost local obscures the definition of x in the outermost local. What if x is also a function defined outside all of the locals — a place that we will
call the top level? The innermost \( x \) hides all definitions that are "farther out" in the nested set of locals.

To summarize the behavior (or meaning, or semantics) of \texttt{local}

\[
\begin{align*}
\text{… top-level definitions …} \\
\text{(local (defs)} \\
\text{expression)}
\end{align*}
\]

becomes

\[
\begin{align*}
\text{… top-level definitions …} \\
\text{… defs … <renamed for uniqueness, or in a new context>} \\
\text{expression <with renaming>}
\end{align*}
\]

until the expression is evaluated, at which point it becomes

\[
\begin{align*}
\text{… top-level definitions} \\
\text{result}
\end{align*}
\]

\textbf{Postlude}

A common complaint about COMP 210 (often heard among people who have taken the course and are now taking COMP 212, 320, or 314) is "we never use any of the stuff that we learned in COMP 210."

Today's lecture is a striking example of the fallacy of that statement. Scheme's local construct is a pure and distilled form of a principle known as \textit{lexical scoping}. The idea was introduced, as far as I know, in Algol 60 (maybe earlier). It is a feature found in most programming languages, including C, C++, Pascal, Modula, ML, Ada, Java, and (in its own quirky way) in Smalltalk.

Understanding \texttt{local} is critical to your ability to program in those languages. The interesting thing about the COMP 210 approach is that we've explained to you how local works—not how to use it, but how it works. You now have the tools to answer some reasonably complex questions about lexical scoping—questions that a simple syntactic introduction to the idea would not make clear.

Because Scheme has such a simple and comprehensible execution model, we can explain complicated features such as local in the same terms that we used to explain algebraic expressions. The knowledge that you gained from this model will come back to help you in all of your programming endeavors, even if you never write another Scheme program after COMP 210.

[The strongest defenders of COMP 210 are the seniors that I see in COMP 412. They are almost unanimous in their praise for the course, even though almost none of them use Scheme in their coursework for COMP 412.]