Last Name:	First Name:

Physics 102 Spring 2005: Test 2—Free Response and Instructions

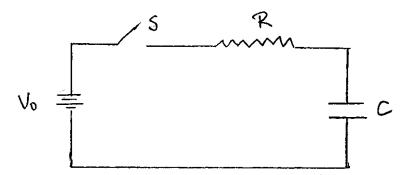
- Print your LAST and FIRST name on the front of your blue book, on this question sheet, the multiple-choice question sheet and the multiple-choice answer sheet.
- TIME ALLOWED 90 MINUTES
- The test consists of two free-response questions and 15 multiple-choice questions.
- The test is graded on a scale of 100 points; the free-response questions are worth a total of 70 points, and the multiple-choice questions account for 30 points.
- Answer the two free-response questions in your blue book. Answer the multiple-choice questions by marking a dark X in the appropriate column and row in the table on the multiple-choice answer sheet.
- Consult no books or notes of any kind. You may use a hand-held calculator in non-graphing, non-programmed mode.
- Do NOT take test materials outside of the class at any time. Return this question sheet along with your blue book and multiple-choice question sheet.
- Write and sign the Pledge on the front of your blue book.

Show your work for the free-response problems, including neat and clearly labeled figures, in your blue book.

Answers without explanation (even correct answers) will not be given credit.

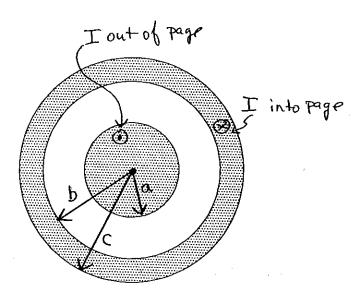
I. (35 pts) The sketch below shows a simple RC circuit. A battery V_0 is connected in series to a resistor R and capacitor C through a switch S. The capacitor is initially uncharged, and at t=0 the switch S is closed. Express your answers in terms of V_0 , R, and C.

- $\int (a)$ Determine I(t), the current through R as a function of time. Sketch I(t) vs t.
- $\varsigma(b)$ Determine Q(t), the charge on C as a function of time. Sketch Q(t) vs. t.
- s (c) Determine $P_V(t)$, the power delivered by the battery as a function of time. Integrate $P_V(t)$ from t=0 to $t=\infty$ to determine the total energy delivered by the battery as the capacitor charges.
- (d) Determine $P_R(t)$, the power dissipated in the resistor as a function of time. Integrate $P_R(t)$ from t = 0 to $t = \infty$ to determine the total energy dissipated in the resistor as the capacitor charges. If the value of R is doubled, how does the total energy dissipated in the resistor change?
- 4 (e) Determine the total energy stored in the capacitor at $t = \infty$.
- 5(f) Compare your answers for energies in (c), (d), and (e). Are the results as expected?

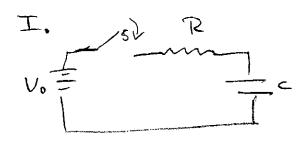


II.(35 pts) The figure below shows the cross section of a long conductor of a type called a coaxial cable. The radius of the inner solid cylinder is a, and the outer cylindrical shell has inner radius b and outer radius c, as shown in the figure below. The conductors carry equal but opposite currents I, with the current in the inner conductor flowing out of the page. The currents are uniformly distributed over the cross-sectional area in each case. The coordinate r measures the distance from the axis of the cylinders. Express your answers in terms of I, a, b, c and possibly other constants.

- 7(a) Determine the magnitude of the current density $|\vec{J}_{inner}|$ in the region r < a. Determine the magnitude of the current density $|\vec{J}_{outer}|$ in the region b < r < c.
- g(b) Determine the magnetic field $\vec{B}(r)$ in the range r < a, being sure to indicate the direction of \vec{B} .
- (c) Determine $\vec{B}(r)$ in the region a < r < b.
- \vec{Q} (d) Determine $\vec{B}(r)$ in the region b < r < c.
- \mathbf{S} (e) Determine $\vec{B}(r)$ in the region r > c.

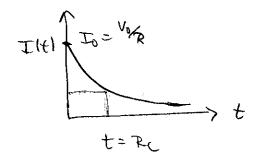


Phys 102 - Exams



Current decays exponentially w/ 7=R(

I (t) = Vo e -t/RC



(b) Q(+) also behaves exponentially, but Q=CVo, that is as t >00 He potential across the capacita = Vo.



We can also find Qit) by untegrating
$$\Xi(t)$$

$$Q(t) = \int_{\mathbb{R}}^{t} \Xi(t')dt' = \frac{1}{N_0} \int_{\mathbb{R}}^{t} e^{-\frac{t}{N}Rc} dt'$$

$$= \frac{V_0}{N_0}(-\aleph c) e^{-\frac{t}{N}Rc} \int_{\mathbb{R}}^{t} e^{-\frac{t}{N}Rc} dt'$$

$$Q(t) = -\frac{V_0}{N_0}(e^{-\frac{t}{N}Rc} - 1)$$

$$Q(t) = \frac{V_0}{N_0}(1 - e^{-\frac{t}{N}Rc}) \quad \text{as above } 1$$

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$$Q(t) = \frac{V_0}{N$$

1 Pp (+) = Vo2 = = >t/pc

Erengy delivered by the battery = energy dissipated in R + energy stored in C So energy conservation works!

Phypiod - Exam 2 Grading Criteria

I. 35 pts total

(a) 5 pts

3 - expression for current

2 - sketch

(b) 5pts

3 - expression for Q(+)

2 - Sketch

(C) 8 pts

3 - expression for Py(t)

5 - integration to get orangy

(d) 8 pts

2 - expression for Petel

5 - integration to get every

1 - NO R dependence.

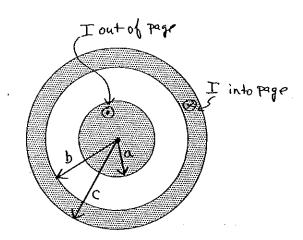
(P) 4 pts

No red to derive expression for the

(1) 5 pts

Give full credit if they understand that everyy should be conserved, even if their expressions for U, Un AVIC don't add up.





(a) I uniformly distributed over area

since area of outer cylindrical shell = 17 (c2-b2)

(b) Because of the symmetry of an infinite wire, we can use Ampere's Law:



Byoms concertice loops, caw in this case.

Direction is Counter-clockwiss loops. O

for 2<9

In the region between the conductors, all of the inner current is enclosed & rome of the outer current is enclosed.

(d) bence

In the region inside the outer conductor, all of the unres current is enclosed a part of the outer current is enclosed. He outer current will subtract from the inner current since they are in opposite directions

$$SR.JO = \mu_0 I - \mu_0 SJ_{outs} JA$$

$$2\pi \Lambda B = \mu_0 I - \mu_0 \left(\frac{T}{\pi(c^2 - b^2)}\right) \left(\frac{2\pi \Lambda^2}{3} - \frac{2\pi b^2}{3}\right)$$

$$2\pi \Lambda B = \mu_0 I - \frac{\mu_0 I}{\pi(c^2 - b^2)} \left(\frac{2\pi \Lambda^2}{3} - \frac{2\pi b^2}{3}\right)$$

$$|\vec{B}| = \frac{h_0 I}{2\pi \Lambda} - \frac{h_0 I}{2\pi (c^2 - b^2)} \left[\chi - \frac{b^2}{2} \right]$$

 $|\vec{B}| = \frac{\lambda_0 T}{2\pi N} \left[1 - \frac{N^2 - b^2}{C^2 - b^2} \right]$

Direction is con logges

PYVCC

$$\left(Abo = \frac{1}{2\pi b} \left[\frac{c_3 - b_2}{c_3 - b_2} \right] \right)$$

(e) for n>c, I and =0 since the total currents are equal and opposite. Hen

1

Phys 103 - Exam 2 Grading Criteria

II. 35 pts

(9) 7 pts

3 - Jinran

4 - Jouter

(b) 8 pts

3- Ampres Law

3 - Correct integral & correct 131 2 - Correct direction of B

(c) 7 pts

2 I andosed = Iinner

2 Amperestan

2 Cornect integral & 181

1 Correct direction of \$

(d) 8 pts

2 I exclosed = Irren - part of I outer

1 Amperos Law

4 Correct Interpral & correct 131 1 Correct direction

(e) 5 pts

They either get it or they don't. I end = 0

PHYSICS 102 EXAM #2 --- MULTIPLE CHOICE

				March 31, 200
e the one alternative	that best completes th	e statement or answers	s the question.	
	shows 3 identical light the switch S is closed?	bulbs connected to a ba	nttery. What happens t	o the brightness of
1 T	S 2	3		
A) The brightr	less increases			
B) The brightr	ess remains the same a	s before the switch is cl	losed	
C) The brightr	ess will decrease mome	entarily then return to i	ts previous level	
D) The brightr	ess will increase mome	ntarily then return to i	ts previous level	
E) The brightr	ess decreases			
	-	-	-	g a linear charge density and cylinders of radii 2b
	B) C/4	C) C/2	D) 4C	E) C

C) f/2.

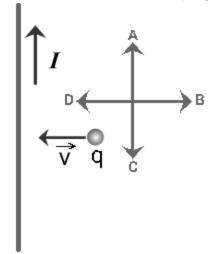
B) 2f.

A) f/4.

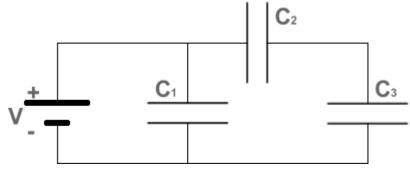
D) f.

E) 4f.

4) The figure below shows a small positive charge q moving toward a long current-carrying wire. Which of the arrows labeled A to D correctly represents the direction of the magnetic force applied on the charge?

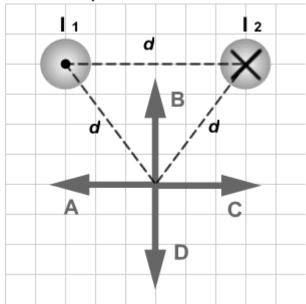


- A) D
- B) B
- C) The force points in a direction perpendicular to the plane of the figure
- D) A
- E) C
- 5) Three capacitors C_1 , C_2 , and C_3 are connected to a battery as shown in the figure below. The three capacitors have equal capcitances. Which capacitor stores the most energy?

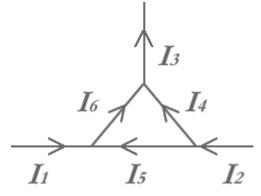


- A) C₂ or C₃. They store the same amount of energy
- B) C₂
- C) C₁
- D) All three capacitors store the same amount of energy
- E) C₃
- 6) A parallel–plate capacitor of capacitance C is connected to a battery of voltage V until it is fully charged. The energy density in the capacitor is then equal to u. If the same capacitor is then connected to a battery of voltage 2V its energy density becomes equal to
 - A) u/4.
- B) 4 u.
- C) 2 u.
- D) u.
- E) u/2.

7) The figure below shows two long wires carrying equal currents I₁ and I₂ flowing in opposite directions. Which of the arrows labeled A to D correctly represents the direction of the magnetic field due to the wires at a point located at an equal distance d from each wire?

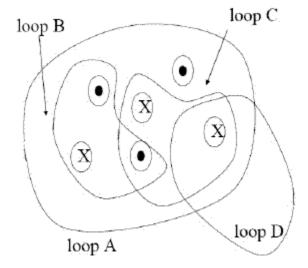


- A) B
- B) D
- C) A
- D) The magnetic field is equal to zero at that point
- E) C
- 8) The figure below shows a junction with currents labeled I_1 to I_6 . Which of the following statements is correct?

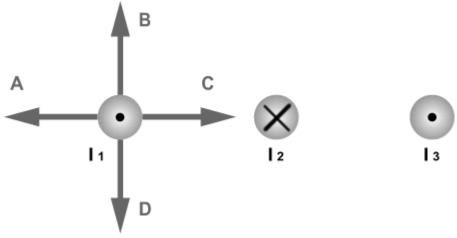


- A) $I_6 + I_5 = I_1$
- B) $I_1 + I_2 = I_6 + I_4$
- C) $I_4 + I_3 = I_6$
- D) $I_2 = I_6 + I_4$
- E) $I_1 + I_3 = I_6 + I_4$

9) Consider six wires coming into or out of the page, all with the same current. Rank the line integral of the magnetic field (from greatest to least) taken counterclockwise around each loop shown.

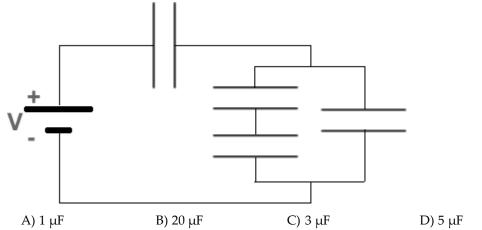


- A) B > C > D > A
- B) B > C = D > A
- C) B > A > C = D
- D) C > B = D > A
- E) C > A > B = D
- 10) The figure below shows 3 long, parallel current-carrying wires. The magnitudes of the currents are equal and their directions are indicated in the figure. Which of the arrows drawn near the wire carrying current 1 correctly indicates the direction of the magnetic force acting on that wire?

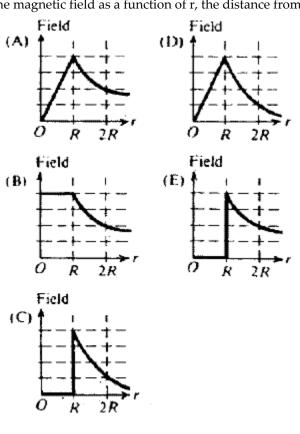


- A) D
- B) A
- C) The magnetic force is equal to zero
- D) B
- E) C

11) What is the equivalent capacitance of the capacitor network shown in the figure below? (All the capacitors have a capacitance $C=5~\mu F$. The voltage of the battery is V=6V.)



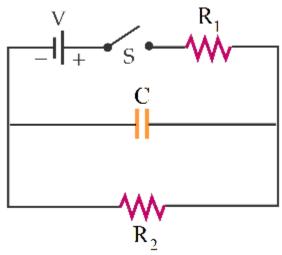
12) A wire of radius R carries a current I uniformly distributed throughout its interior. Which plot below best represents the magnitude of the magnetic field as a function of r, the distance from the center of the wire?



- A) A
- B) B
- C) C
- D) D
- E) E

E) 10 μF

For questions 13 – 15, refer to the circuit below.



- 13) What is the current through R_2 as $t\!\to\!\infty\!?$
 - A) $\frac{V}{R_1 + R_2}$

- D) 0
- E) ∞

- 14) What is the current through C at t = 0?
 - A) $\frac{V}{R_1+R_2}$ B) $\frac{V}{R_2}$
- C) $\frac{V}{R_1}$
- D) 0
- E) ∞

- 15) What is the charge on the capacitor as $t \rightarrow \infty$?
 - A) V C
 - B) $(\frac{V}{R_1}R_2)C$
 - C) $(\frac{V}{R_2}R_1)C$
 - D) $(\frac{V}{R_1+R_2}R_2)C$
 - E) 0

Physics 102 Spring 2005: Test 2—Multiple-Choice Answers

	A	В	С	D	Е
1					
3					
3					
4					
5 6					
6					
7					
Q					
9					
10					
11					
12					
13					
14					
15					

Answer Key
Testname: EXAM2_MATERIAL_USED_1

- 1) A 2) E 3) D 4) E 5) C 6) B 7) A 8) B 9) C 10) B 11) C 12) A

- 13) A 14) C
- 15) D