

Physics 102 Spring 2007: Suggested Problems # 7

1. Problem 28-35. (+10 pts)

i. +3 pts - Correct value for the speed of the particle from kinetic energy.

$$v = \sqrt{\frac{2K}{m}}$$

ii. +6 pts - Correct application of Newton's 2nd law to find B .

$$B = \frac{mv}{qr}$$

$$B_{max} = \frac{m}{qR} \sqrt{\frac{2K_{max}}{m}} = 3.54T$$

iii. +1 pt - Correct numerical answer above.

28-35

Given the kinetic energy, we could find the speed

$$K = \frac{1}{2}mv^2 \rightarrow v = \sqrt{\frac{2K}{m}}$$

We could find the maximum Magnetic field required to keep maximum energy particle in orbit.

$$qvB = mv^2/r \rightarrow r = \frac{mv}{qB} \rightarrow B = \frac{mv}{qr}$$

$$\text{so } B_{\max} = \frac{mv_{\max}}{qR} = \frac{m}{qR} \sqrt{\frac{2K_{\max}}{m}}$$

$$B_{\max} = \frac{1}{qR} \sqrt{2K_{\max} \cdot m}$$

$$\Rightarrow B_{\max} = \frac{\sqrt{2(6 \times 10^4 \text{ eV})(1.6 \times 10^{-27} \text{ kg})}}{2(1.6 \times 10^{-19} \text{ C})(0.1 \text{ m})} = 4(1.67 \times 10^{-27} \text{ kg})^{1/2}$$

$$B_{\max} = 3.54 \text{ T}$$

α -particle of smaller KE require a smaller \vec{B} field.