

# MECH 401

## Mechanical Design Applications

Fundamentals Section – Master Notes

Spring 2004  
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Rice University

## Course Information

- Meeting time
  - T-Th 8:00 – 9:15
  - DH 1042
- Prerequisites
  - MECH 311 or CIVI 300
- Texts
  - Mechanical Engineering Design by Shigley, Mischke, and Budynas
- Goals
  - Provide design skills to support MECH 407/408 projects
  - Understand the application of engineering analysis to common machine elements
  - Enhance your ability to solve practical design problems using free body diagrams, Mohr's circle, beam analysis, etc.
- M. K. O'Malley, PhD
  - MEB 216
  - Phone: 3545
  - [omalleym@rice.edu](mailto:omalleym@rice.edu)
  - Office hours:
    - Monday 11:00 AM – 12:00 PM
  - Fundamentals
- D. M. McStravick, PhD, P.E.
  - MEB 219
  - Phone: 2427
  - [dmcs@rice.edu](mailto:dmcs@rice.edu)
  - Office hours:
    - TBA
  - Applications

## Syllabus

- General policies
- (20%) Homework
  - Late homework is not accepted
  - Neatness counts!
- (10%) In-class mini-tests (6 total)
- (20%) Project

## Overview and introduction of design of machine elements

- Two primary phases of design
  - ① Inventive phase – creative aspect
  - ② Engineering phase – understanding of physical reality aspect
    - ① makes a design unique or clever (MECH 407/408)
    - ② makes a design work
- This course will focus on 2<sup>nd</sup> aspect, making our designs work

## “Understanding of physical reality”

- Theoretical results
- Empirical results
- Theory helps us understand physical phenomena so that we can address design at a fundamental level
- Theory often falls short, however, in describing complex phenomena, so we must use empirical results

## Systems of Units

- Appendix lists units (English, SI), conversion factors, and abbreviations
- Unit
  - A specified amount of a physical quantity by which through comparison another quantity of the same kind is measured
  - Examples?
    - Length, time, temperature
- 2 basic systems of units
  - U.S. customary foot-pound-second system (fps)
  - International System of Units (SI)

## Primary dimensions

- Sufficient to conceive of and measure other dimensions
- Examples?

## Secondary dimensions

- Measured in terms of primary dimensions
- Examples?

## U.S. customary

- Foot-pound-second (fps)
- Inch-pound-second (ips)
- FPS:
  - Force – pound-force
  - $1000 \text{ lbf} = 1 \text{ kilopound} = 1 \text{ kip}$
  - Derived unit of mass is  $\text{lbf}\cdot\text{s}^2/\text{ft}$  (slug)

## SI (mLt)

- Mass, length, and time
- $m - \text{kg}$
- $L - m$
- $t - s$
- F is secondary (Newtons)
- $1 \text{ N} \sim 1 \text{ apple}$
- $F = ma$
- $1 \text{ N} = 1 \text{ kg}\cdot\text{m}/\text{s}^2$



## Methodology

- Solving machine component problems
  - Step 1
    - Define/understand
  - Step 2
    - Define/synthesize the structure
    - ID interactions
    - Draw diagrams
  - Step 3
    - Analyze/solve using:
      - Appropriate assumptions
      - Physical laws
      - Relationships
      - Rules
  - Step 4
    - Check – is the answer reasonable?

## Homework format

- Start each problem on a new page
- One side of sheet only
- Use straight-edge, work neatly
- Known:
  - Problem statement
  - Schematic
  - Given data
  - Material properties
- Find:
  - Concisely state what is to be determined
- Solution:
  - Assumptions
  - Design decisions
  - Equations (make number substitutions last)
  - Comments (when appropriate)

## Introduction to reliability engineering

- We cannot assume that all the quantities that we utilize in failure analysis are deterministic quantities
  - "We know their values absolutely!"
- In many cases, especially in manufacturing, this is NOT the case
  - A part dimension that is supposed to be 1" in diameter might vary between 0.95 and 1.05 inches due to variation in machining process (tool wear)
- Statistics and random variable methods enable designers to deal with variable quantities
  - Reliability Engineering

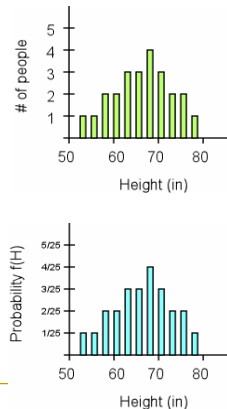
## Definitions

- Random (stochastic) variable
  - A real-valued set of numbers that result from a random process or are descriptive of a random relationship
- For example, if I were to construct a list of everybody's height in this class...
  - Then height,  $H$ , would be considered a random variable

Sample #	H (height in inches)
1	
2	
3	
4	

## Height example

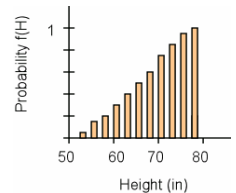
- Let's say there are 25 people in this class.
- Construct a histogram to represent the data
- If we divide the (# of people) axis by the total number of people sampled, then we have
  - Probability density function (pdf)
  - PDF gives the probability that a random variable will have a certain value
  - Same shape as the histogram



## Height example

- If we integrate this "function", we get the cumulative distribution function (cdf)
  - Gives the probability (likelihood) that a random variable will be less than or equal to a given value
  - For a random variable  $x$ ,
 
$$\lim_{x \rightarrow \infty} F(x) = 1$$
  - For a discrete random variable,

$$F(x_i) = \sum_{x_j \leq x_i} f(x_j)$$



## Characterizing random variables

- A random variable is not a scalar, but rather a vector
- In this deterministic case, we can say
  - $x = 63.5$  inches
- This is a scalar, since it has only a single value
- In the stochastic case, we know that the variable  $x$  can take on many values
  - $x = 63.5, 68.7, 62.1$ , etc
- We define the discrete random variable  $\mathbf{x}$  to be a vector of the samples  $x_1, x_2, \dots, x_n$ 
  - We refer to  $\mathbf{x}$  as the variate
    - $$\mathbf{x} = \begin{bmatrix} x_1 \\ \vdots \\ x_n \end{bmatrix}$$
  - Note, in this sense, a vector can be considered a collection of numbers, not a quantity with direction and magnitude
  - It is helpful to have some scalar quantities that characterize the random variable vector
    - Direction and magnitude won't do the trick!

## Scalar quantities to characterize $\mathbf{x}$

- Mean
 
$$\hat{\mu} \equiv \frac{x_1 + x_2 + \dots + x_n}{N} = \frac{1}{N} \sum_{i=1}^N x_i$$
  - A measure of the central value of a distribution
- Standard deviation
 
$$\hat{\sigma} \equiv \left[ \frac{1}{N-1} \sum_{i=1}^N (x_i - \hat{\mu})^2 \right]^{1/2}$$
  - A measure of the dispersion or distribution of data
  - Note – this is most useful as a comparative measure
    - By itself, it's not particularly useful!
  - Some people use  $1/N$  instead of  $1/(N-1)$ , but  $1/(N-1)$  typically gives better results for small  $N$
- The notation for mean and standard deviation of a variate are as follows:

$$\mathbf{x} = (\hat{\mu}, \hat{\sigma})$$

## Reliability Engineering, Cont.

### Terminology

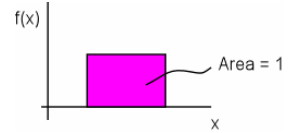
- Population
  - The total set of elements in which we are interested
- Sample
  - A randomly selected subset of the total population on which measurements are taken

### Describing the shape of a distribution

- Uniform
  - Normal
  - Log Normal
  - Weibull
- } We'll look at these

## Uniform distribution

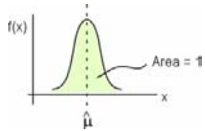
- Simplest
- All elements have the same value
- Area equal to 1 implies that all samples in the given range of  $x$  have the same value of  $f(x)$ , where  $f(x)$  describes the distribution



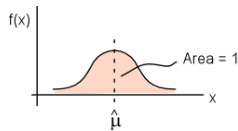
## Normal distribution

- Also called Gaussian distribution

$$f(x) = \frac{1}{\hat{\sigma}\sqrt{2\pi}} e^{\left[-\frac{1}{2}\left(\frac{x-\hat{\mu}}{\hat{\sigma}}\right)^2\right]}$$



Small standard deviation ( $\hat{\sigma}$ )



Large standard deviation ( $\hat{\sigma}$ )

## Notation

- Normal distribution with mean and standard deviation:

$$\mathbf{x} = \mathbf{N}(\hat{\mu}, \hat{\sigma})$$

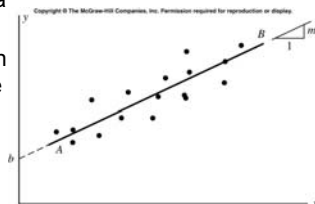
- This IS a complete characterization
- CDF of Normal (Gaussian) Distribution cannot be found in closed form
- Generalized description of normal CDF:

$$\mathbf{z} = \frac{\mathbf{x} - \hat{\mu}}{\hat{\sigma}}$$

Note:  $F(x) = \int_{-\infty}^x f(u) du$

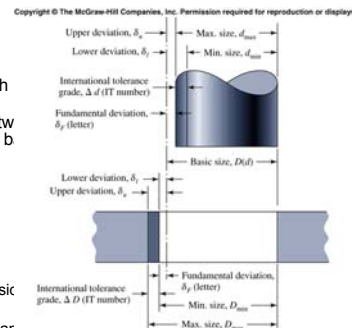
## Linear Regression

- Obtaining a best-fit to a set of data points
- Linear regression when best fit is a straight line
- Correlation coefficient tells you how good the fit is



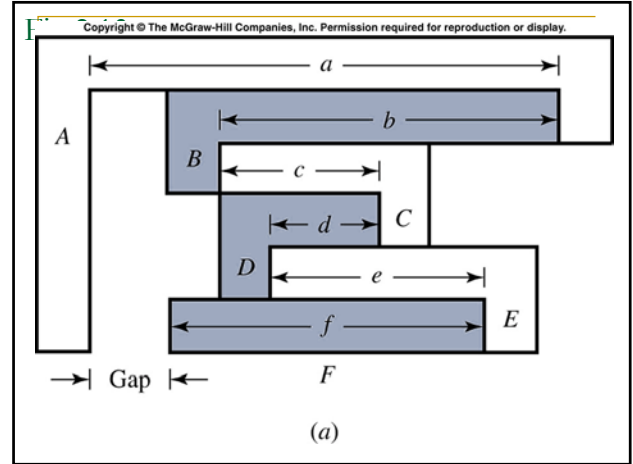
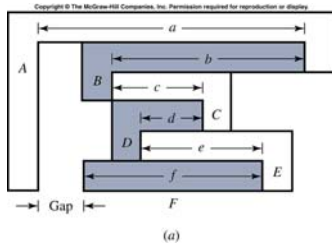
## Limits and fits

- Capital letters – hole
- Lowercase letters – shaft
- Basic size – same for both members of the fit
- Deviation – difference between a size and corresponding basic size
- Upper deviation
  - Max-size
- Lower deviation
  - Min-size
- Fundamental deviation
  - Either upper or lower, whichever is closer to basic
- Tolerance
  - Difference between max ar... min deviations



## Dimensions and tolerances

- Nominal size
- Basic size
- Limits
- Tolerance
- Clearance
- Interference
- Allowance



## Materials and Processes

- Must always make “things” out of materials
- Must be able to manufacture this “thing”
- Topics first introduced in Materials Science course (MSCI 301)
- How do we determine the properties of a material?
  - Tables
- How were these values determined?
  - Generally via destructive testing

## Material properties

- Listed in tables
- Statistical variation
- Values listed are minimums
- Best data from testing of prototypes under intended loading conditions

## Material parameters

- Parameters of interest in material selection for design?
  - Strength
  - Stiffness
  - Weight

PRIMARY CONCERNS

- Toughness
- Conductivity
- Thermal
- Corrosion resistance

## Primary parameters of interest in material selection

- Strength
  - Amount of load (or weight, or force) a part can take before breaking or bending
- Stiffness
  - Amount of deflection or deformation for a given load
- Weight
- All of these depend on geometry
  - EXTENSIVE values
- We would like to derive results that are independent of size (geometry)
  - INTENSIVE values

## Extensive vs. Intensive values

- Extensive
  - Weight (kg)
  - Strength (N)
  - Stiffness (N/m)
- Intensive
  - Density ( $\text{kg/m}^3$ )
  - Yield strength or Ultimate Strength ( $\text{N/m}^2$ )
  - Modulus of Elasticity ( $\text{N/m}^2$ )

## How do we determine these values?

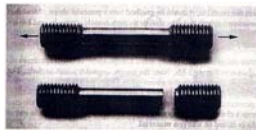
- Types of quasistatic material testing
  - Tension
  - Compression
  - Bending
  - Torsion

## Tensile tests specimens

What is the difference between these specimens?



Mild ductile steel tensile test specimen



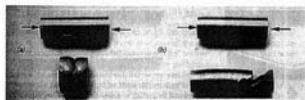
Brittle cast iron tensile test specimen

## Tensile testing

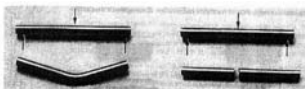
- Best for general case
- Why?
  - Uniform loading and uniform cross-section generate uniform stress
  - Compression poses stability problems (buckling)
  - Torsion and bending impose non-uniform stress

## Other test specimens – Ductile and Brittle

Compression



Bending

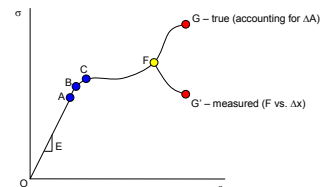


Torsion



## Stress-Strain ( $\sigma$ - $\epsilon$ ) Curves

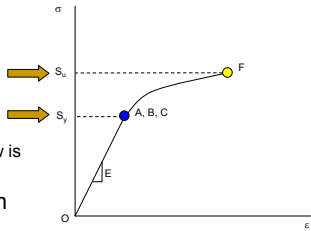
- Point A – Proportional limit
- Point B – Elastic limit
- Point C – Yield point
  - Usually defined by permanent set of  $\epsilon = 0.002$  (0.2% offset)
- For purposes of design, we often assume A~B~C, and call this the yield point
- Slope of O-A = E
  - Young's Modulus
  - Modulus of elasticity
  - Like stiffness
- Point F – Onset of failure
- Point G, G' - Fracture



## Important design considerations

### ■ $S_y$ = Yield strength

- It is the stress level...
  - That will result in permanent set
  - At which material undergoes marked decrease in stiffness
  - At which Hooke's Law is no longer valid



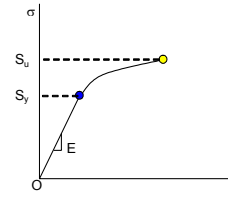
### ■ $S_u$ = Ultimate strength

- Stress level that will result in fracture

## Ductile vs. Brittle Material Behavior

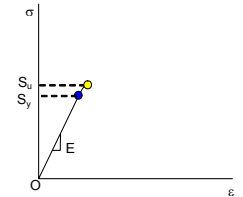
### ■ Ductile material

- Sustains significant plastic deformation prior to fracture



### ■ Brittle material

- No significant plastic deformation before fracture



## Ductile vs. Brittle Material Behavior

- The only true means of determining if a material is ductile or brittle is by testing it (tensile test)
- Note: The same alloy can be either ductile or brittle, depending upon temperature and/or how it was formed
- Some general indications of brittle behavior
  - Glass, ceramic, and wood
  - Cast ferrous alloys
  - Materials in extreme cold temperatures
  - Also, if you can't find  $S_y$  in a handbook (only  $S_u$  given)

## Fatigue testing – measuring endurance

- Most machines are loaded cyclically
  - Any piece of rotating machinery
- Strength decreases over time
  - "Fatigue strength" depends on number of cycles and the material



### ■ How to test?

- Use a rotating beam
- More often vary axial loading over time

## Common metals in machine design

### ■ Magnesium

- Specific stiffness ~ 25 MPa/(kg/m<sup>3</sup>)
- Extremely light (~1/5 steel)
- Extremely flammable



### ■ Aluminum (very common)

- Specific stiffness ~ 26
- Stiffness-to-weight and strength-to-weight comparable to steel
- 1/3 stiffness of steel
- 1/3 density of steel

## More metals...

### ■ Gray cast iron

- Specific stiffness ~ 15
- Decent strength
- Used where casting makes sense and weight doesn't matter
  - Gears, engine blocks, brake disks and drums

### ■ Brass, bronze

- Generally soft
- Good for bearings (bronze)



## More metals...

### ■ Titanium

- Specific stiffness ~ 26
- Excellent strength-to-weight
- Non-magnetic
- Non-corrosive (implants)
- Can be cast
- Expensive

### ■ Ductile cast iron

- Stronger than gray cast iron
- Heavy-duty gears, automobile door hinges



## More metals...

### ■ Stainless steel

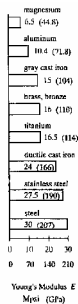
- Non-magnetic
- Much less corrosive than steel
- Difficult to machine

### ■ Steel

- Specific stiffness ~ 27
- Excellent fatigue properties
- Good stiffness-to-weight
- Better alloys have excellent strength-to-weight
  - Chromoly bicycle frames



## Comparison of Young's Modulus for various metals



## Question...

- Does all steel have the same strength?
- Does all steel have the same stiffness?
- Strength ( $S_y$ ,  $S_u$ ) depends on alloy and state
- Stiffness (E) depends only on metal type
  - i.e., E is a property of the metal and does not change with alloy or state

## So what affects the strength of a metal?

### ■ Two primary forms –

- Alloying
- Crystal state

### ■ Metal alloys

- Adding certain elements in trace amounts to a metal can significantly change its strength
- Since the alloying elements are present in trace amounts, they don't significantly alter modulus (stiffness) or density

## Alloying

### ■ Steel – Primary alloying elements:

- Manganese
- Nickel
- Chromium
- Molybdenum
- Vanadium

### ■ The alloy is identified by AISI/SAE or ASTM numbering system

- AISI – American Iron and Steel Institute
- SAE – Society of Automotive Engineering
- ASTM – American Society for Testing and Materials

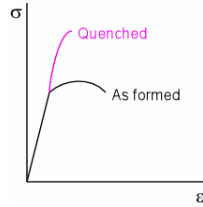


## Altering crystal state

- Crystal state of steel can be altered by heat treatment or cold working

### Quenching

- Heat to very high (~1400°F) temp and cool rather suddenly by immersion in water
- Creates crystal structure called martensite which is extremely strong but brittle



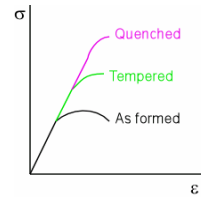
## More methods...

### Tempering

- Reheat to moderate temperature and cool slowly
- Adds ductility at the expense of decreased strength

### Annealing

- Resets the alloy to original low strength, ductile state
- Reheat alloy above critical temperature and allow to cool slowly



## More methods...

### Normalizing

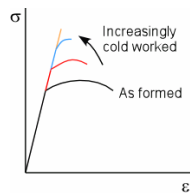
- Between tempering and annealing

### Cold working

- Another means of increasing strength at the expense of ductility

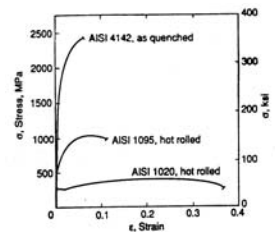
### Hot working

- Reheating as the metal is deformed to maintain ductility



## Question

- If you're going to have a piece of metal machined, would you rather use a cold worked or hot worked metal?



## Steel numbering systems

- Used to define alloying elements and carbon content

### 1<sup>st</sup> two digits

- Indicate principal alloying elements

### Last 2 digits

- Indicate amount of carbon present
- In 100ths of a percent

## Steel number systems

### Plain carbon steel

- 1<sup>st</sup> digit – 1
- 2<sup>nd</sup> digit – 0
- No alloys other than carbon are present
- AISI 1005-1030: Low-carbon steels
- AISI 1035-1055: Medium-carbon steels
- AISI 1060-1085: High-carbon steels
- AISI 11xx series adds sulphur
  - Improves machinability
  - Called free-machining steels
- Not considered alloys –
  - Sulphur does not improve mechanical properties
  - Makes it brittle

## Steel number systems

- Alloy steels
  - Have various elements added in small quantities
  - Improve material's
    - Strength
    - Hardenability
    - Temperature resistance
    - Corrosion resistance
    - Other...
  - Nickel –
    - Improve strength without loss of ductility
    - Enhances case hardenability
  - Molybdenum
    - In combination with nickel and/or chromium
    - Adds hardness
    - Reduces brittleness
    - Increases toughness
  - Other alloys used to achieve specific properties

## Steel numbering systems

- Tool steels
  - Medium- to high- carbon alloy steels
  - Especially formulated to give:
    - Very high hardness
    - Wear resistance
    - Sufficient toughness to resist shock loads experienced in machining
- Stainless steels
  - Alloy steels with at least 10% chromium
  - Improved corrosion resistance over plain or alloy steels

## Steel numbering systems

- Martensitic stainless steels
  - 11.5 to 15% Cr and 0.15 to 1.2% C
  - Magnetic
  - Can be hardened by heat treatment
  - Cutlery
- Ferritic stainless steel
  - Over 16% Cr and low C content
  - Magnetic
  - Soft
  - Ductile
  - Not heat treatable
  - Cookware
- Both martensitic and ferritic called 400 series

## Steel numbering systems

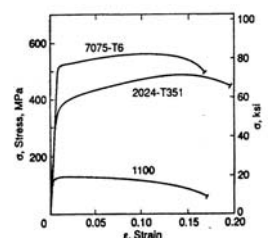
- Austenitic stainless steel
  - 17 to 25% Cr and 10 to 20% nickel
  - Better corrosion resistance (due to Ni)
  - Nonmagnetic
  - Excellent ductility and toughness
  - Cannot be hardened except by cold working
  - 300 series
- 300 series very weldable
- 400 series less so

## Aluminum alloys

- Principal alloying elements
  - Copper
  - Manganese
  - Silicon
  - Zinc
- Alloys are designated by the Aluminum Association numbering system

## Aluminum alloys, cont.

- Aluminum alloys are also heat-treatable, as designated by the –T classification in the AA numbering system



## Aluminum alloys

- Wrought-aluminum alloys

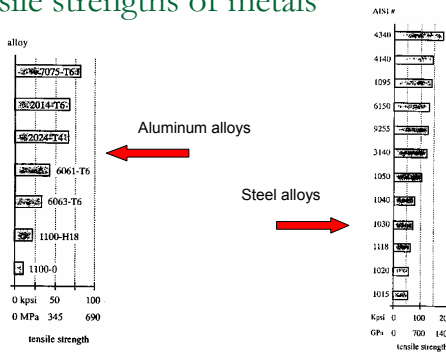
- ❑ Available in wide variety of stock shapes
  - I-beams, angles, channels, bars, etc
- ❑ 1<sup>st</sup> digit indicates principal alloying element
- ❑ Hardness indicated by a suffix containing a letter and up to 3 numbers
- ❑ Most commonly available and used in machine design applications:
  - 2000 series
  - 6000 series

## Aluminum alloys

- 2024

- Oldest alloy
  - Among the most machinable
  - One of the strongest Al alloys
  - High fatigue strength
  - Poor weldability and formability
- 6061
- Widely used in structural applications
  - Excellent weldability
  - Lower fatigue strength than 2024
  - Easily machined and popular for extrusion
- 7000 series
- Aircraft aluminum
  - Strongest alloys

## Tensile strengths of metals



Look-up tables for  
Material properties  
(in the appendix)

AGE-SEX	TREATMENT	3			
		10 mg/kg SPRINT®	10 mg/kg SPRINT®	10 mg/kg SPRINT®	10 mg/kg SPRINT®
30/50	Q1	291 (40)	259 (32)	245 (32)	245 (32)
	Q2	314 (50)	306 (48)	321 (49)	321 (49)
	Q3	317 (50)	317 (50)	317 (50)	317 (50)
	Q4	245 (30)	266 (37)	271 (35)	271 (35)
80/0	Q1	317 (48)	317 (48)	317 (48)	317 (48)
	Q2	317 (48)	317 (48)	317 (48)	317 (48)
	Q3	271 (43)	271 (43)	271 (43)	271 (43)
	Q4	271 (43)	271 (43)	271 (43)	271 (43)
110/0	Q1	317 (48)	317 (48)	317 (48)	317 (48)
	Q2	317 (48)	317 (48)	317 (48)	317 (48)
	Q3	271 (43)	271 (43)	271 (43)	271 (43)
	Q4	271 (43)	271 (43)	271 (43)	271 (43)
80/50	Q1	317 (48)	317 (48)	317 (48)	317 (48)
	Q2	317 (48)	317 (48)	317 (48)	317 (48)
	Q3	271 (43)	271 (43)	271 (43)	271 (43)
	Q4	271 (43)	271 (43)	271 (43)	271 (43)
120/5	Q1	317 (48)	317 (48)	317 (48)	317 (48)
	Q2	317 (48)	317 (48)	317 (48)	317 (48)
	Q3	271 (43)	271 (43)	271 (43)	271 (43)
	Q4	271 (43)	271 (43)	271 (43)	271 (43)
114/1	Q1	317 (48)	317 (48)	317 (48)	317 (48)
	Q2	317 (48)	317 (48)	317 (48)	317 (48)
	Q3	271 (43)	271 (43)	271 (43)	271 (43)
	Q4	271 (43)	271 (43)	271 (43)	271 (43)
41/0	Q1	317 (48)	317 (48)	317 (48)	317 (48)
	Q2	317 (48)	317 (48)	317 (48)	317 (48)
	Q3	271 (43)	271 (43)	271 (43)	271 (43)
	Q4	271 (43)	271 (43)	271 (43)	271 (43)