



COMP 412  
FALL 2009

*Parsing Wrap Up  
+ Lab 2 Overview*

*Comp 412*

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# LR( $k$ ) versus LL( $k$ )

## Finding Reductions

LR( $k$ )  $\Rightarrow$  Each reduction in the parse is detectable with

- $\rightarrow$  the complete left context,
- $\rightarrow$  the reducible phrase, itself, and
- $\rightarrow$  the  $k$  terminal symbols to its right

generalizations of LR(1) and LL(1) to longer lookaheads

LL( $k$ )  $\Rightarrow$  Parser must select the reduction based on

- $\rightarrow$  The complete left context
- $\rightarrow$  The next  $k$  terminals

Thus, LR( $k$ ) examines more context

*The question is, do languages fall in the gap between LR( $k$ ) and LL( $k$ )?*



## LR(1) versus LL(1)

The following LR(1) grammar has no LL(1) counterpart

0	<i>Goal</i>	→	<i>S</i>
1	<i>S</i>	→	<i>A</i>
2			<i>B</i>
3	<i>A</i>	→	( <i>A</i> )
4			<u><i>a</i></u>
5	<i>B</i>	→	( <i>B</i> >
6			<u><i>b</i></u>

- It requires an arbitrary lookahead to choose between *A* & *B*
- An LR(1) parser can carry the left context (the '(' s) until it sees *a* or *b*
- The table construction will handle it
- In contrast, an LL(1) parser cannot decide whether to expand *Goal* by *A* or *B*  
→ *No amount of massaging the grammar will resolve this problem*

- The Canonical Collection has 18 sets of LR(1) Items
  - It is not a simple grammar
  - It is, however, LR(1)

More formally, the language described by this LR(1) grammar cannot be described with an LL(1) grammar. In fact, the language has no LL(*k*) grammar, for finite *k*.



# LR(1) versus LL(1)

## The Canonical Collection of Sets of LR(1) Items

- cc<sub>0</sub> [*Goal* → • *S*, EOF], [*S* → • *A*, EOF], [*S* → • *B*, EOF] [*A* → • ( *A* ), EOF],  
[*A* → • *a*, EOF], [*B* → • ( *B* ≥, EOF ], [*B* → • *b*, EOF ],
- cc<sub>1</sub> [*Goal* → *S* •, EOF]
- cc<sub>2</sub> [*S* → *A* •, EOF]
- cc<sub>3</sub> [*S* → *B* •, EOF]
- cc<sub>4</sub> [*A* → • ( *A* ),  ) ], [*A* → ( • *A* ), EOF ], [*A* → • *a*,  ) ], [*B* → • ( *B* ≥,  ≥ ],  
[*B* → ( • *B* ≥, EOF ], [*B* → • *b*,  ≥ ]
- cc<sub>5</sub> [*A* → *a* •, EOF]
- cc<sub>6</sub> [*B* → *b* •, EOF]
- cc<sub>7</sub> [*A* → ( *A* • ), EOF]
- cc<sub>8</sub> [*B* → ( *B* • ≥, EOF ]

cc<sub>4</sub> is goto(cc<sub>0</sub>, ( )

0	<i>Goal</i>	→	<i>S</i>
1	<i>S</i>	→	<i>A</i>
2			<i>B</i>
3	<i>A</i>	→	( <u><i>A</i></u> )
4			<u><i>a</i></u>
5	<i>B</i>	→	( <i>B</i> ≥
6			<u><i>b</i></u>
			<i>s</i>



# LR(1) versus LL(1)

And, the rest of it ...

cc<sub>9</sub> [A→•( A ), ], [A→ (•A ), ], [A→•a, ], [B→• (B ≥, ≥],  
[B→ (• B ≥, ≥], [B→•b, ≥]

cc<sub>10</sub> [A→a•, )]

cc<sub>11</sub> [B→b•, ≥]

cc<sub>12</sub> [A→( A )•, EOF]

cc<sub>13</sub> [B→ ( B ≥•, EOF]

cc<sub>14</sub> [A→ ( A •), )]

cc<sub>15</sub> [B→ ( B • ≥, ≥]

cc<sub>16</sub> [A→ ( A )•, )]

cc<sub>17</sub> [B→ ( B ≥•, ≥]

0	Goal	→	S
1	S	→	A
2			B
3	A	→	( A )
4			a
5	B	→	( B ≥
6			b

# LR(1) versus LL(1)

	EOF	(	)	<u>a</u>	<u>≥</u>	<u>b</u>	<i>S</i>	<i>A</i>	<i>B</i>
<i>s</i> <sub>0</sub>		<i>s</i> <sub>4</sub>		<i>s</i> <sub>5</sub>		<i>s</i> <sub>6</sub>	1	2	3
<i>s</i> <sub>1</sub>	acc								
<i>s</i> <sub>2</sub>	<i>r</i> <sub>2</sub>								
<i>s</i> <sub>3</sub>	<i>r</i> <sub>3</sub>								
<i>s</i> <sub>4</sub>		<i>s</i> <sub>9</sub>		<i>s</i> <sub>10</sub>		<i>s</i> <sub>11</sub>		7	8
<i>s</i> <sub>5</sub>	<i>r</i> <sub>5</sub>								
<i>s</i> <sub>6</sub>	<i>r</i> <sub>7</sub>								
<i>s</i> <sub>7</sub>			<i>s</i> <sub>12</sub>						
<i>s</i> <sub>8</sub>					<i>s</i> <sub>13</sub>				
<i>s</i> <sub>9</sub>				<i>s</i> <sub>10</sub>		<i>s</i> <sub>11</sub>		14	15
<i>s</i> <sub>10</sub>			<i>r</i> <sub>5</sub>						
<i>s</i> <sub>11</sub>					<i>r</i> <sub>7</sub>				
<i>s</i> <sub>12</sub>	<i>r</i> <sub>4</sub>								
<i>s</i> <sub>13</sub>	<i>r</i> <sub>6</sub>								
<i>s</i> <sub>14</sub>			<i>s</i> <sub>16</sub>						
<i>s</i> <sub>15</sub>					<i>s</i> <sub>17</sub>				
<i>s</i> <sub>16</sub>			<i>r</i> <sub>4</sub>						
<i>s</i> <sub>17</sub>					<i>r</i> <sub>6</sub>				

0	<i>Goal</i>	→	<i>S</i>
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5	<i>B</i>	→	( <i>B</i> <u><i>≥</i></u> )
6			<u><i>b</i></u>

- Notice how sparse the table is.
  - Goto has 7 of 54
  - Action has 23 of 108
- Notice rows & columns that might be combined.



## LR( $k$ ) versus LL( $k$ )

### Finding Reductions

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generalizations of  
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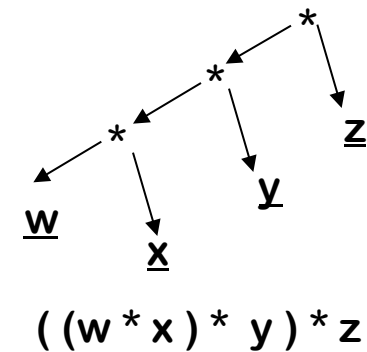
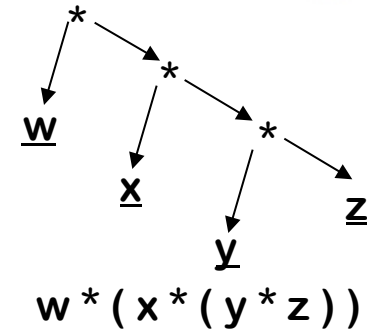
*"... in practice, programming languages do not actually seem to fall in the gap between LL(1) languages and deterministic languages"*

*J.J. Horning, "LR Grammars and Analysers", in Compiler Construction, An Advanced Course, Springer-Verlag, 1976*

# Left Recursion versus Right Recursion



- Right recursion
  - Required for termination in top-down parsers
  - Uses (on average) more stack space
  - Produces right-associative operators
- Left recursion
  - Works fine in bottom-up parsers
  - Limits required stack space
  - Produces left-associative operators
- Rule of thumb
  - Left recursion for bottom-up parsers
  - Right recursion for top-down parsers

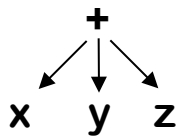




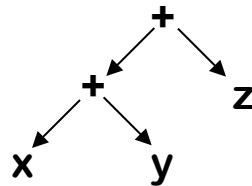
# Associativity

What difference does it make?

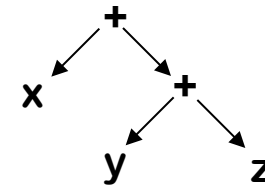
- Can change answers in floating-point arithmetic
- Can change opportunities for optimization
- Consider  $x+y+z$



*Ideal operator*



*Left association*



*Right association*

What if  $y+z$  occurs elsewhere? Or  $x+y$ ? or  $x+z$ ?

The compiler may want to change the "shape" of expressions

- What if  $x = 2$  &  $z = 17$ ? Neither left nor right exposes 19.
- Best shape is function of surrounding context

# Error Detection and Recovery

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## Error Detection

- Recursive descent
  - Parser takes the last else clause in a routine
  - Compiler writer can code almost any arbitrary action
- Table-driven LL(1)
  - In state  $s_i$  facing word  $x$ , entry is an error
  - Report the error, valid entries in row for  $s_i$  encode possibilities
- Table-driven LR(1)
  - In state  $s_i$  facing word  $x$ , entry is an error
  - Report the error, shift states in row encode possibilities
  - Can precompute better messages from LR(1) items

# Error Detection and Recovery

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## Error Recovery

- Table-driven LL(1)
  - Treat as missing token, e.g. ')',  $\Rightarrow$  expand by desired symbol
  - Treat as extra token, e.g., 'x - + y',  $\Rightarrow$  pop stack and move ahead
- Table-driven LR(1)
  - Treat as missing token, e.g. ')',  $\Rightarrow$  shift the token
  - Treat as extra token, e.g., 'x - + y',  $\Rightarrow$  don't shift the token

Can pre-compute sets of states with appropriate entries...



# Error Detection and Recovery

One common strategy is “hard token” recovery

Skip ahead in input until we find some “hard” token, e.g. ‘;’

- ‘;’ separates statements, makes a logical break in the parse
- Resynchronize state, stack, and input to point after hard token
  - LL(1): pop stack until we find a row with entry for ‘;’
  - LR(1): pop stack until we find a state with a reduction on ‘;’
- Does not correct the input, rather it allows parse to proceed

```
NT ← pop()
repeat until Table[NT,‘;’] ≠ error
  NT ← pop()
token ← NextToken()
repeat until token = ‘;’
  token ← NextToken()
```

*Resynchronizing an LL(1) parser*

Comp 412, Fall 2009

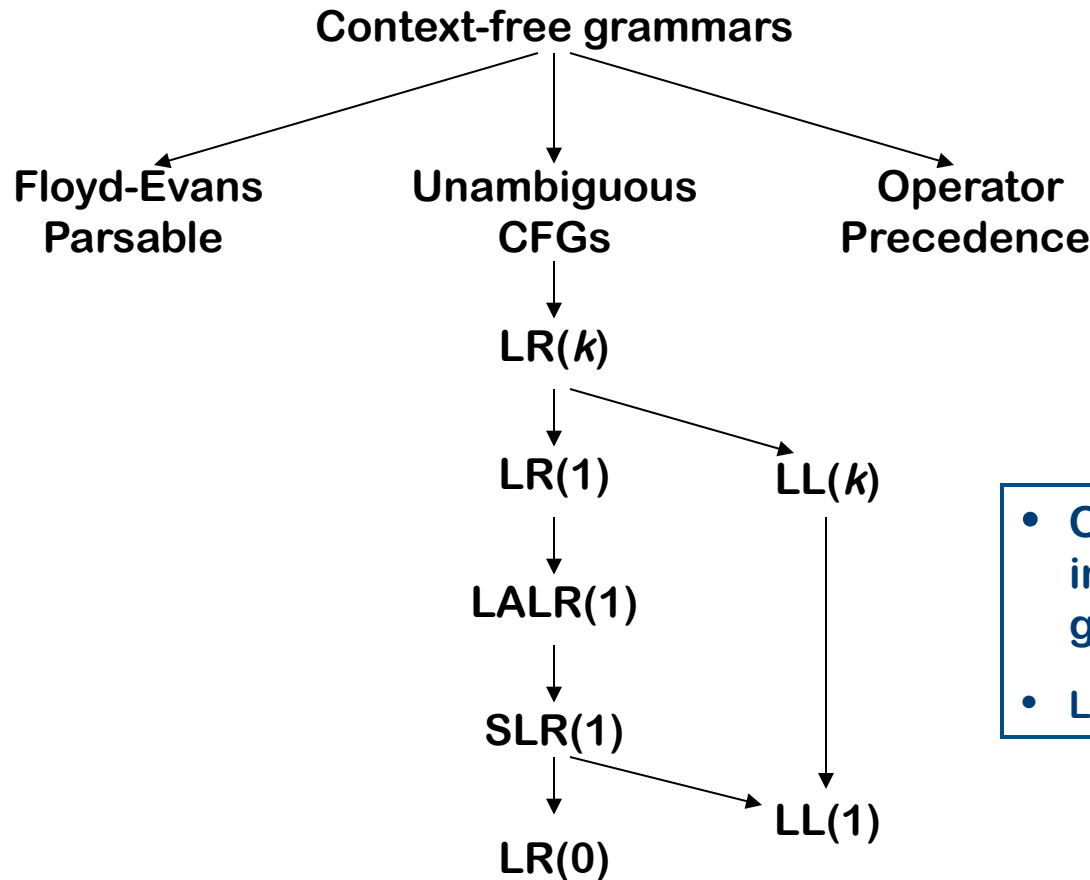
```
repeat until token = ‘;’
  shift token
  shift  $s_e$ 
  token ← NextToken()
reduce by error production
// pops all that state off stack
```

*Resynchronizing an LR(1) parser*

11



# Hierarchy of Context-Free Grammars



- Operator precedence includes some ambiguous grammars
- LL(1) is a subset of SLR(1)

*The inclusion hierarchy for context-free grammars*

## Lab 2 Overview: An LL(1) Parser Generator

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You will build a program to generate LL(1) parse tables

- Input is a modified form of Backus-Naur Form (MBNF)
- Output is a parse table and some auxiliary data structures
  - Both a pretty (human-readable) version and the C declarations
- You will write:
  - A hand-coded scanner for MBNF
  - A hand-coded, recursive descent parser for MBNF
  - A table generator (First, Follow, First<sup>+</sup> sets)
- Interim deadlines to keep you on track
  - Want you to make progress at a steady rate
- Documents will be online by Wednesday
- Skeleton parser ready in about a week, with its own docs

# Beyond Syntax



There is a level of correctness that is deeper than grammar

```
fie(a,b,c,d)
  int a, b, c, d;
  { ... }
fee() {
  int f[3],g[0],
    h, i, j, k;
  char *p;
  fie(h,i,"ab",j, k);
  k = f * i + j;
  h = g[17];
  printf("<%s,%s>.\n",
    p,q);
  p = 10;
}
```

What is wrong with this C program?  
*(let me count the ways ...)*

To generate code, we need to understand its meaning !

Beyond Syntax



There is a level of correctness that is deeper than grammar

```
fie(a,b,c,d)
  int a, b, c, d;
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fee() {
  int f[3],g[0],
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  fie(h,i,"ab",j, k);
  k = f * i + j;
  h = g[17];
  printf("<%s,%s>.\n",
    p,q);
  p = 10;
}
```

What is wrong with this C program?

*(let me count the ways ...)*

- declared g[0], used g[17]
- wrong number of args to fie()
- "ab" is not an int
- wrong dimension on use of f
- undeclared variable q
- 10 is not a character string

All of these are "deeper than syntax"

# Beyond Syntax



To generate code, the compiler needs to answer many questions

- Is "x" a scalar, an array, or a function? Is "x" declared?
- Are there names that are not declared? Declared but not used?
- Which declaration of "x" does each use reference?
- Is the expression "x \* y + z" type-consistent?
- In "a[i,j,k]", does a have three dimensions?
- Where can "z" be stored? (*register, local, global, heap, static*)
- In "f ← 15", how should 15 be represented?
- How many arguments does "fie()" take? What about "printf ()" ?
- Does "\*p" reference the result of a "malloc()" ?
- Do "p" & "q" refer to the same memory location?
- Is "x" defined before it is used?