

## CHBE470 – Process Dynamics and Control – Fall 2007

### Homework Set 6

**Assigned:** Wednesday, October 22

**Due:** Wednesday, October 29

**Note:** Please staple your papers and include your name in the first page

**Problem 1:** Consider the general closed-loop block diagram with  $G_c(s) = K_c(1 + 3/s)$ ,  $G_f(s) = 1$ ,  $G_m(s) = 2$  and  $G_p(s) = 1/(0.2s^2 + 0.4s + 1)$ . Using the Routh-Hurwitz stability criterion, determine the stability of the closed-loop system when  $K_c = 2$ .

**Problem 2:** Consider the general closed-loop block diagram with  $G_c(s) = K_c$ ,  $G_f(s) = G_m(s) = 1$  and  $G_p(s) = 1/(s + 1)^3$ . Find the value of  $K_c$  for which the system is on the verge of instability. The controller is then replaced by a PD controller, for which the transfer function is  $G_c(s) = K_c(1 + \tau_D s)$ . If  $K_c = 10$ , determine the range of  $\tau_D$  for which the system is stable.

**Problem 3:** Consider the general closed-loop block diagram with  $G_c(s) = K_c$ ,  $G_f(s) = 1$ ,  $G_m(s) = 1/(s + 1)$  and  $G_p(s) = 1/(s + 1)^3$ .

- Determine the value of  $K_c$  above which the system is unstable
- Determine the value of  $K_c$  for which two of the roots are on the imaginary axis and determine the values of these imaginary roots.